

Name \_\_\_\_\_ No Calculators. Present neatly. Score \_\_\_\_\_.

1)

Find the dimensions of the rectangle of largest area that can be inscribed in a circle of radius  $r$ .

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2)

If a resistor of  $R$  ohms is connected across a battery of  $E$  volts with internal resistance  $r$  ohms, then the power (in watts) in the external resistor is

$$P = \frac{E^2 R}{(R + r)^2}$$

If  $E$  and  $r$  are fixed but  $R$  varies, what is the maximum value of the power?

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3)

The top and bottom margins of a poster are each 6 cm and the side margins are each 4 cm. If the area of printed material on the poster is fixed at  $384 \text{ cm}^2$ , find the dimensions of the poster with the smallest area.

Your work:

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NO ANSWERS ON THIS PAGE

Name \_\_\_\_\_ No Calculators. Present neatly. Score \_\_\_\_\_.

1)

An object with weight  $W$  is dragged along a horizontal plane by a force acting along a rope attached to the object. If the rope makes an angle  $\theta$  with a plane, then the magnitude of the force is

$$F = \frac{\mu W}{\mu \sin \theta + \cos \theta}$$

where  $\mu$  is a constant called the coefficient of friction. For what value of  $\theta$  is  $F$  smallest?

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2)

A poster is to have an area of  $180 \text{ in}^2$  with 1-inch margins at the bottom and sides and a 2-inch margin at the top. What dimensions will give the largest printed area?

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3)

Find the area of the largest rectangle that can be inscribed in the ellipse  $x^2/a^2 + y^2/b^2 = 1$ .

Your work:

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NO ANSWERS ON THIS PAGE