

(* Quiz 26 | AP Calculus AB | Prepared by D. Shubleka*)

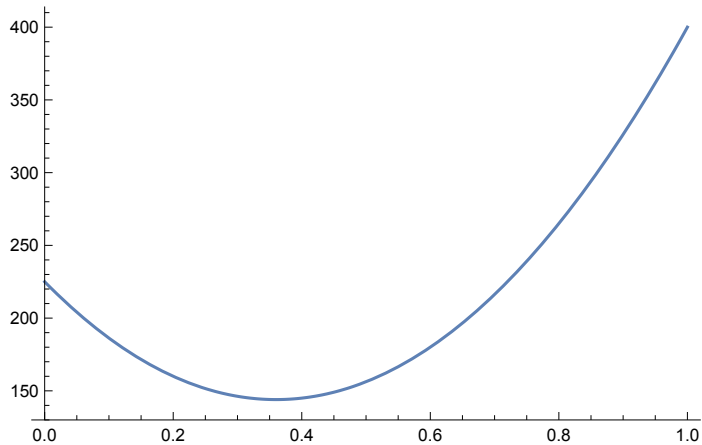
(* Problem 1 *)

```
y[t_] := 20 t;
```

```
x[t_] := -15 + 15 t;
```

```
Q[t_] := (20 t)^2 + (-15 + 15 t)^2;
```

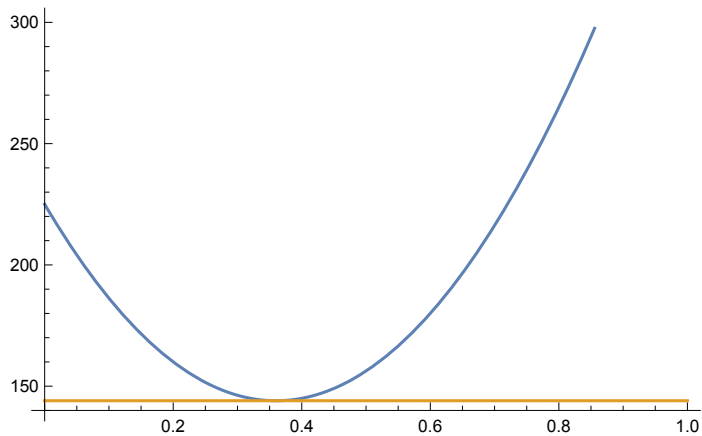
```
Plot[Q[t], {t, 0, 1}]
```



```
Simplify[Q'[t]]
```

```
50 (-9 + 25 t)
```

```
Plot[{Q[t], Q[9/25]}, {t, 0, 1}]
```



The minimum of the square of the distance occurs at $t = 9/25$. This corresponds to 2:21:36PM. Distance itself will be at a minimum at this time as well. In this problem we should remember to justify the identified point is a minimum (and not a maximum or neither) by using the First Derivative Test or the Second Derivative Test for Global Extrema.)

(* Problem 2 *)

```
f[x_] := 1 / (x^2 - 9);
```

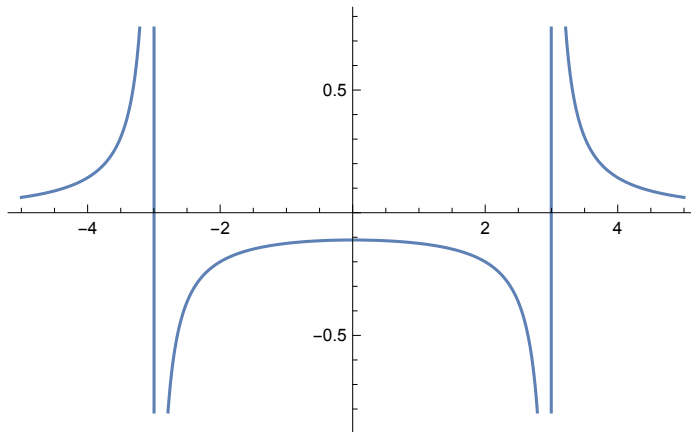
Simplify[f' [x]]

$$-\frac{2x}{(-9+x^2)^2}$$

Simplify[f'' [x]]

$$\frac{6(3+x^2)}{(-9+x^2)^3}$$

Plot[f[x], {x, -5, 5}]



Comment: construct tables for each derivative; identify local extrema (one local max, no global extrema), inflection points (none), asymptotes (two VA, one HA), intercepts, ID behavior, and concavity.

(* Problem 1 *)

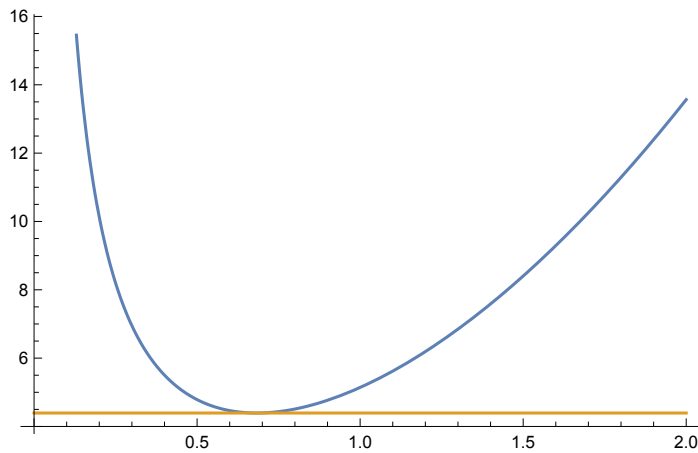
Suppose the volume is 1 cubic unit.

Q[r_] := Pi r^2 + 2 Pi r (1 / (Pi r^2));

Simplify[Q' [r]]

$$-\frac{2}{r^2} + 2\pi r$$

```
Plot[{Q[r], Q[(1 / (Pi))^(1 / 3)]}, {r, 0, 2}]
```



The precise critical number is $r = (V / \text{Pi})^{1/3}$. The other dimension is $h = V / (\text{Pi } r^2) = (V / \text{Pi})^{1/3}$. Use the First or Second Derivative for Global Extrema to justify that the critical number gives an absolute minimum.

(* Problem 2 *)

```
g[x_] := x^2 / (x^2 + 9);
```

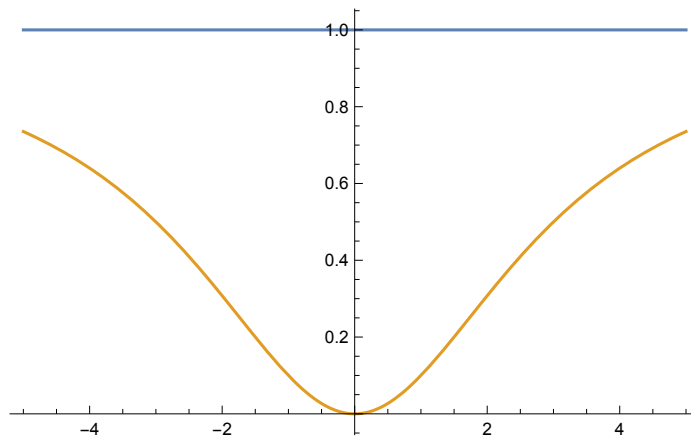
```
Simplify[g' [x]]
```

$$\frac{18x}{(9+x^2)^2}$$

```
Simplify[g'' [x]]
```

$$-\frac{54(-3+x^2)}{(9+x^2)^3}$$

```
Plot[{1, g[x]}, {x, -5, 5}]
```



Comment: construct tables for each derivative; identify local extrema (one local and global min), inflection points (two), asymptotes (no VA, one HA), intercepts, ID behavior, and concavity.