

Name \_\_\_\_\_ No Calculators. Present neatly. Score \_\_\_\_\_.

1.

Find  $y'$  if  $y = \ln(x^2 + y^2)$

Your work:

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Find  $y'$  if  $y = \ln(x^2 + y^2)$

$$\frac{dy}{dx} = \frac{1}{x^2 + y^2} \left( 2x + 2y \frac{dy}{dx} \right)$$

$$\frac{dy}{dx} - \frac{2y}{x^2 + y^2} \frac{dy}{dx} = \frac{2x}{x^2 + y^2}$$

$$\frac{dy}{dx} \left( 1 - \frac{2y}{x^2 + y^2} \right) = \frac{2x}{x^2 + y^2}$$

$$\frac{dy}{dx} \left( \frac{x^2 + y^2 - 2y}{x^2 + y^2} \right) = \frac{2x}{x^2 + y^2}$$

$$\frac{dy}{dx} = \frac{2x}{x^2 + y^2 - 2y}$$

**Name** \_\_\_\_\_ **No Calculators. Present neatly. Score** \_\_\_\_\_.

1.

Find  $y'$  if  $\ln xy = y \sin x$

Your work:

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Find  $y'$  if  $\ln xy = y \sin x$

$$\frac{1}{xy} \left( y + x \frac{dy}{dx} \right) = y \cos x + \frac{dy}{dx} \sin x$$

$$\frac{1}{x} + \frac{1}{y} \frac{dy}{dx} - \frac{dy}{dx} \sin x = y \cos x$$

$$\frac{dy}{dx} \left( \frac{1}{y} - \sin x \right) = y \cos x - \frac{1}{x}$$

$$\frac{dy}{dx} \left( \frac{1 - y \sin x}{y} \right) = \frac{xy \cos x - 1}{x}$$

$$\frac{dy}{dx} = \frac{y(xy \cos x - 1)}{x(1 - y \sin x)}$$