

Name SHUBLEKA / KEY No Calculators. Present neatly. Score _____.

Find the limit.

1)

$$\lim_{h \rightarrow 0} \frac{\sqrt[4]{16+h} - 2}{h} \quad f(x) = \sqrt[4]{x} \quad @ \quad x=16; \text{ since } f(16)=2$$

$$= \frac{d}{dx} (x^{1/4}) \Big|_{x=16} = \frac{1}{4} \cdot x^{-3/4} \Big|_{x=16} = \frac{1}{4 \cdot 8} = \frac{1}{32}$$

2)

$$\lim_{x \rightarrow 1} \frac{x^{17} - 1^{17}}{x - 1} = \frac{d}{dx} (x^{17}) \Big|_{x=1} = 17 \cdot x^{16} \Big|_{x=1} = 17$$

3)

$$\lim_{\theta \rightarrow \pi/3} \frac{\cos \theta - (0.5)^{\cos \pi/3}}{\theta - \pi/3} = \frac{d}{d\theta} (\cos \theta) \Big|_{\theta=\pi/3} = -\sin \theta \Big|_{\theta=\pi/3} = -\frac{\sqrt{3}}{2}$$

NOTE: $f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$

or $f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$