

Name \_\_\_\_\_ No Calculators. Present neatly. Score \_\_\_\_\_.

1)

Let  $r(x) = f(g(h(x)))$ , where  $h(1) = 2$ ,  $g(2) = 3$ ,  $h'(1) = 4$ ,  $g'(2) = 5$ , and  $f'(3) = 6$ . Find  $r'(1)$ .

2)

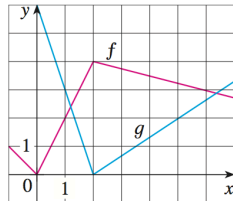
If the equation of motion of a particle is given by  $s = A \cos(\omega t + \delta)$ , the particle is said to undergo *simple harmonic motion*.

- (a) Find the velocity of the particle at time  $t$ .
- (b) When is the velocity 0?

3)

If  $f$  and  $g$  are the functions whose graphs are shown, let  $u(x) = f(g(x))$ ,  $v(x) = g(f(x))$ , and  $w(x) = g(g(x))$ . Find each derivative, if it exists. If it does not exist, explain why.

- (a)  $u'(1)$
- (b)  $v'(1)$
- (c)  $w'(1)$



Your work:

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1)

Suppose  $f$  is differentiable on  $\mathbb{R}$  and  $\alpha$  is a real number.  
 Let  $F(x) = f(x^\alpha)$  and  $G(x) = [f(x)]^\alpha$ . Find expressions  
 for (a)  $F'(x)$  and (b)  $G'(x)$ .

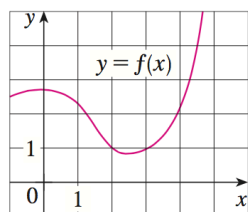
2)

The displacement of a particle on a vibrating string is given by  
 the equation  $s(t) = 10 + \frac{1}{4} \sin(10\pi t)$  where  $s$  is measured in  
 centimeters and  $t$  in seconds. Find the velocity of the particle  
 after  $t$  seconds.

3)

If  $f$  is the function whose graph is shown, let  $h(x) = f(f(x))$   
 and  $g(x) = f(x^2)$ . Use the graph of  $f$  to estimate the value  
 of each derivative.

(a)  $h'(2)$       (b)  $g'(2)$



Your work: