Present neatly on separate paper. Justify for full credit. No Calculators.

Name \_\_\_\_\_ Score \_\_\_\_ A (30 minutes) **x5** For questions 1 through 5, determine whether the series converges or diverges. 1)

 $\sum_{n=1}^{\infty} \frac{n^2 + 1}{n^3 + 1}$ 

2)

 $\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{n+1}}$ 

3)

$$\sum_{n=1}^{\infty} \ln\left(\frac{n}{3n+1}\right)$$

4)

$$\sum_{n=1}^{\infty} \frac{n^{2n}}{(1+2n^2)^n}$$

5)

 $\sum_{n=1}^{\infty} \frac{(-5)^{2n}}{n^2 9^n}$ 

6)

State the following.

- (a) The Test for Divergence
- (b) The Integral Test
- (c) The Comparison Test

Present neatly on separate paper. Justify for full credit. No Calculators.

Name \_\_\_\_\_ Score \_\_\_\_ F (30 minutes) **x5** For questions 1 through 5, determine whether the series converges or diverges. 1)

 $\sum_{n=1}^{\infty} \frac{n}{n^3 + 1}$ 

## 2)

 $\sum_{n=1}^{\infty} \frac{n^3}{5^n}$ 

## 3)

 $\sum_{n=2}^{\infty} \frac{1}{n\sqrt{\ln n}}$ 

## 4)

 $\sum_{n=1}^{\infty} \frac{\cos 3n}{1+(1.2)^n}$ 

5)

$$\sum_{n=1}^{\infty} \, (-1)^{n-1} \, \frac{\sqrt{n}}{n+1}$$

6)

- a) What is an absolutely convergent series? What can you say about such a series?
- b) What is a *p*-series? Under what circumstances is it convergent?
- c) What is a geometric series? Under what circumstances is it convergent? What is its sum?