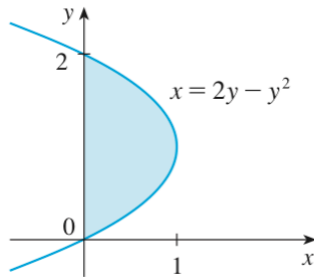


Present neatly on separate paper. Justify for full credit. No Calculators.

Name \_\_\_\_\_ Score \_\_\_\_\_ <25 minutes **Weight: x8**

1)

The area of the region that lies to the right of the  $y$ -axis and to the left of the parabola  $x = 2y - y^2$  (the shaded region in the figure) is given by the integral  $\int_0^2 (2y - y^2) dy$ . (Turn your head clockwise and think of the region as lying below the curve  $x = 2y - y^2$  from  $y = 0$  to  $y = 2$ .) Find the area of the region.



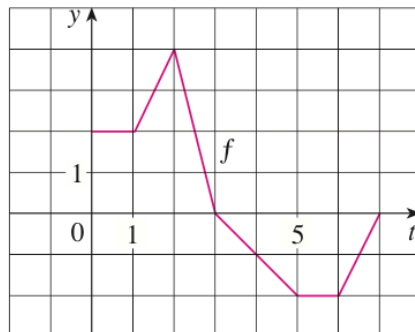
2) Evaluate the integral:

$$\int_0^1 \frac{4}{t^2 + 1} dt$$

3)

Let  $g(x) = \int_0^x f(t) dt$ , where  $f$  is the function whose graph is shown.

- Evaluate  $g(0)$ ,  $g(1)$ ,  $g(2)$ ,  $g(3)$ , and  $g(6)$ .
- On what interval is  $g$  increasing?
- Where does  $g$  have a maximum value?
- Sketch a rough graph of  $g$ .



4) Evaluate the integral or explain why it does not exist.

$$\int_0^{\pi/2} \cos x \sin(\sin x) dx$$