

Problem 1

$$y = \frac{x-1}{x+1}$$

$$// x - 2y = 2 \rightarrow y = \frac{x-2}{2}$$

$$\frac{dy}{dx} = \text{slope} = \frac{1}{2}$$

$$\frac{dy}{dx} = \frac{(x+1) \cdot 1 - 1(x-1)}{(x+1)^2} = \frac{2}{(x+1)^2}$$

$$\frac{2}{(x+1)^2} = \frac{1}{2} \rightarrow (x+1)^2 = 4$$

$$x+1 = 2 \quad \text{or} \quad x+1 = -2$$

$$x = 1, x = -3$$

$$(1, 0), m = \frac{1}{2} \rightarrow y - 0 = \frac{1}{2}(x - 1) \rightarrow y = \frac{1}{2}x - \frac{1}{2}$$

$$(-3, 2), m = \frac{1}{2} \rightarrow y - 2 = \frac{1}{2}(x + 3) \rightarrow y = \frac{1}{2}x + \frac{7}{2}$$

Problem 2

$$y = x^2 - 5x + 4$$

$$x - 3y = 5 \rightarrow y = \frac{x-5}{3}$$

$$\text{slope of normal line} = \frac{1}{3}$$

$$\text{tangent line slope} = -3$$

$$\frac{dy}{dx} = 2x - 5 = -3 \rightarrow x = 1, y = 0$$

$$y - 0 = \frac{1}{3}(x - 1) \rightarrow y = \frac{1}{3}x - \frac{1}{3}$$