

Present neatly on separate paper. Justify for full credit. No Calculators.

Name _____ Score _____ ~15 minutes

1. In each case draw a graph of $f(x)$ on the interval $[0, 4]$. [4 points]

a)

Jump discontinuity at $x = 2$ and does not satisfy the conclusion of the IVT.

b)

Jump discontinuity at $x = 2$ and satisfies the conclusion of the IVT on $[0, 4]$.

c)

Infinite one-sided limits at $x = 2$ and does not satisfy the conclusion of the IVT.

d)

Infinite one-sided limits at $x = 2$ and satisfies the conclusion of the IVT on $[0, 4]$.

2.

For a) through d), find the limit or explain why it does not exist. [6 points]

a)

$$\lim_{h \rightarrow 0} \frac{\sin(2h)(1 - \cos h)}{h^2}$$

b)

$$\lim_{x \rightarrow \frac{\pi}{3}} \frac{2 \cos^2 x + 3 \cos x - 2}{2 \cos x - 1}$$

c)

$$\lim_{x \rightarrow -2} \frac{x^3 + 8}{x^2 + 6x + 8}$$

d)

$$\lim_{\theta \rightarrow \frac{\pi}{4}} \left(\frac{1}{\tan \theta - 1} - \frac{2}{\tan^2 \theta - 1} \right)$$

e) Find the value(s) of c for which the limit exists.

$$\lim_{x \rightarrow 1} \frac{x^2 + 3x + c}{x - 1}$$

f) Find the value(s) of c for which the limit exists.

$$\lim_{x \rightarrow 1} \left(\frac{1}{x - 1} - \frac{c}{x^3 - 1} \right)$$