Mathematica Labs | Denis Shubleka Subject: Calculus Topic: Inflection Points

Goal: Use Mathematica to identify inflection points.

Task 1

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By definition, f(x) has an inflection point at (a, f(a)) as long as
three
conditions are satisfied:
(1) f(x) is continuous at x=a.
(2) f'(x) does not change sign at x=a.
(3) f"(x) changes sign at x=a.
We define a cubic function:
f[x] := 2x^2 - x^3
The second derivative is also a polynomial (degree 1), hence any sign
change
of f''(x) would occur at a point where f''(x)=0. We find the root(s), by
searching near x=1, as we suspect the inflection is somewhere between
x=0
and x=2.
FindRoot[f''[x] == 0, {x, 1}]
We assign a variable to the (x, y) pair that describes the inflection
point.
inflectionpt = \{x, f[x]\} /. %
, and then plot the original function, as well as the inflection point:
Plot[f[x], \{x, -1, 3\}, Epilog \rightarrow \{PointSize[0.03], Blue, Point[inflectionpt]\}]
From the graph we confirm that the identified point is in fact an
inflection
point. To confirm a sign change in the second derivative, test whether
the
product of the second deratives evaluated on either side is negative:
f''[0.65] * f''[0.67] < 0
Although not necessary in this example, we can also verify that the
first
derivative maintains its sign ('- to -' or '+ to +'):
f'[0.65] * f'[0.67] > 0
We conclude this task by plotting f(x), f'(x), and f''(x) in the same
window:
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Related Exercises/Notes:

ap-calc.github.io