

Subject: Calculus

Topic: Derivatives Graphically

Goal: Use the Manipulate command to visualize the derivative as a function

Task 1

The interactive window shows that as h approaches zero, the graph of the quotient approaches that of $-\sin[x]$, verifying that the derivative of $\cos[x]$ is $-\sin[x]$. Feel free to alter the expression below using another function.

```
Manipulate[Plot[{ $\frac{\cos[x+h] - \cos[x]}{h}$ ,  $-\sin[x]$ }, {x,  $-2\pi$ ,  $2\pi$ }, {h, 1, 0.01}]
```

Now we plot $y=2^x$ and its tangent line at the point $(1, 2)$, and zoom in closely at $(1,2)$. What do you notice?

```
f[x_] := 2x;  
Manipulate[Plot[{f[x], f'[1] * (x - 1) + f[1]}, {x, 1 - m, 1 + m},  
  Frame → True, Axes → False, Epilog → {Red, Point[{1, 2}]},  
  GridLines → {Range[0, 3, 0.05], Range[-1, 10, 0.2]}, GridLinesStyle → Gray,  
  FrameTicks → None, Filling → {1 → {2}}}, {m, 1, "zoom"}, 1, 0.1]
```

Related Exercises/Notes:
