**AP Calculus Summative Review** 

Name

## **NO CALCULATOR**

Please use a separate sheet of paper to complete the following problems. Be sure to show all of your work.

1. a. Find 
$$\lim_{x \to 5} \frac{x^2 - 3x - 10}{x^2 - 10x + 25}$$

b. Find 
$$\lim_{h\to 0} \frac{\sqrt{2x+2h}-\sqrt{2x}}{h}$$

- 2. If there are two functions f(x) and g(x) with both  $\lim_{x\to\infty} f(x) = \infty$  and  $\lim_{x\to\infty} g(x) = \infty$ , give an example for f (x) and g(x) for which  $\lim_{x\to\infty} \frac{f(x)}{g(x)} = \frac{4}{3}$ .
- 3. If  $f(x) = x^3 3x + 4$ , explain why there exists an x-value, c, on the interval (-3, 0) such that f(c) = 0. Be complete and specific and name any theorem that you use.

4.

a. Let 
$$f(x) = \tan^3 6x$$
, find  $f'(x)$ 

b. Let 
$$f(x) = x^3 \cdot e^{\cos(2x)}$$
, find  $f'(x)$ 

$$\underline{c}$$
. Let  $f(x) = \log_2 x^3$ , find  $f'(x)$ 

d. Find 
$$\frac{dy}{dx}$$
 if  $y = cos^{-1}(\sqrt{x})$ 

- 5. Use logarithmic differentiation to find  $\frac{dy}{dx}$  when  $y = x^{\sqrt{x}}$ .
- 6. Let m(x) =  $\frac{g(x)}{1+f(x)}$ . Using the numerical values in the table, find the value of each of the derivatives below. Justify each answer

X	f (x)	g (x)	f '(x)	g '(x)
0	1	1	6	1/3
1	3	0	-1/3	-8/3

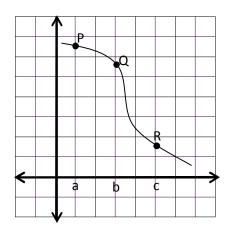
7. Use the one of the correct versions of the definition of the derivative to find derivative of the function  $y = \sqrt{3x-2}$  . THEN find an equation of the <u>tangent</u> line at x = 9.

- 8. Calculate the equation of the normal line to  $y = \sin(x) + \cos(x)$  at = .
- 9. If  $x^3 y^3 4 = 4$ , find the value of  $\frac{d^2 y}{dx^2}$  at the point (-2, -1). Note: you do not need to simplify your  $\frac{d^2y}{dx^2}$  algebraically before substituting.
- 10. If the graph of f (x) is shown below, arrange in the following in ascending order (smallest first)

A) f'(a) B) f'(b) C) f'(c) D) Slope of secant line PQ

E) The slope of secant line 
$$\stackrel{\longleftrightarrow}{\sf QR}$$
 F)  $\frac{f(a)-f(c)}{a-c}$ 

F) 
$$\frac{f(a)-f(c)}{a-c}$$



11. Let 
$$f(x) = \begin{cases} \sqrt{-x} & \text{if } x < 0 \\ 3 - x & \text{if } 0 \le x < 3 \\ (3 - x)^2 & \text{if } x > 3 \end{cases}$$

Evaluate each limit, if it exists.

$$\lim_{x\to 0^+} f(x) =$$

$$\lim_{x\to 0^-} f(x) =$$

11. The graph below contains a function and its derivative. Label which is which. Justify your answer using only the characteristics of the graph, without referring to the possible degree of the function or the derivative. You many add and label any points which might be helpful if necessary.

