ALGEBRA AND TRIGONOMETRY SELF-DIAGNOSTIC EXAM

<u>Do not</u> use a calculator, book, or notes for any part of the exam. The suggested time to complete the exam is 90 minutes; however, make sure to attempt every problem.

1. Simplify:
$$\frac{\left(x^2yz^{-2}\right)^3}{\left(xy^2z\right)^2}$$

- 2. An equivalent algebraic expression to $m^{(4x-7y)}$ is:
- 3. Factor: $2y^4 32x^4$.

4. Simplify:
$$\frac{x}{x^2 + 5x + 6} - \frac{2}{x^2 + 3x + 2}$$

5. After rationalizing the denominator of $\frac{3}{1-\sqrt{2}}$, an equivalent expression is:

6. Simplify:
$$\frac{\sqrt[5]{64x^5y^{-1}}}{\sqrt[5]{2y^4}}$$

- 7. Simplify: $32^{4/5}$
- 8. Solve for x: $(x+a)(x-b) = x^2 1$
- 9. After clearing the numerator and denominator of fractions, $\frac{2x + \frac{1}{4}}{3x \frac{1}{5}}$ is equivalent to:
- 10. Given: $1-5x = \sqrt{6x-7}$, find all real values of x which satisfy the equation.
- 11. The radius of a circular fountain is 10 ft. A sidewalk of uniform width is constructed around the outside of the fountain and has an area of 69π ft². How wide is the sidewalk?
- 12. A train leaves a station and travels north at a speed of 75 mph. Two hours later, a second train leaves on a parallel track traveling north at 125 mph. How far from the station will the faster train overtake the slower train?
- 13. Use "completing the square" to rewrite $x^2 4x + 3 = 0$ in the form $(x c)^2 = d$.
- 14. Write an equation for y in terms of x assuming that y is proportional to x and y = 42 when x = 6.

15. Given the system of equations
$$\begin{cases} 4x + 2y = 14 \\ 2x - 8y = 8 \end{cases}$$
, find the value of y:

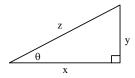
16. Given:
$$f(x) = 3 + x^2$$
, find $f(x+h) - f(x)$.

17. Given:
$$f(x) = \sqrt{x^2 - 9}$$
, find $f(x - 3)$.

- 18. What is the domain of the function $y = \frac{5}{\sqrt{Q-x}}$?
- 19. Find the slope-intercept form of the line through (1,4) and (3,-2).
- 20. Temperature T in degrees Fahrenheit is given by $T = \frac{9}{5}C + 32$ where C is temperature in degrees Celsius. What is the Celsius equivalent to 77°F?
- 21. Given g(2) = 4 and f(x) = x/2, find f(g(2)).
- 22. Find the point(s) of intersection of the curves $x^2 + y^2 = 1$ and y + x = 0.
- 23. Given $f(x) = -3x^2 18x 15$, find the vertex and the maximum or minimum value.
- 24. Solve for *x*: $2 \le 5 2x \le 22$
- 25. Solve for *x*: $|3x-2|-6 \ge 0$
- 26. Solve for *x*: $x^2 35 \le 1$
- 27. Find the roots of $f(x) = (x^2 7x + 12)^2$ and state the multiplicity of each.
- 28. Solve for *x*: $e^{-4x} = e$.
- 29. Solve for x: $3^{4x+1} 5 = 22$.
- 30. Is the point $(\frac{-\sqrt{35}}{6}, \frac{-1}{6})$ inside, outside, or on the unit circle?
- 31. Find z, given that:

$$\sin(z) = -\cos(z)$$
 and $\frac{3\pi}{2} \le z \le 2\pi$

- 32. Given $f(x) = \sin(4x)$, find $f\left(\frac{\pi}{4}\right)$.
- 33. Given: $2\sin(x) = 1$, and $90^{\circ} \le x \le 180^{\circ}$. Find x.
- 34. Complete the trigonometric identity: $\sin(\pi \theta) =$
- 35. Given $\sin(x) = -3/5$ and x is in Quadrant III, find $\tan(x)$.
- 36. If a circle has radius 10 ft, what central angle θ corresponds to an arc of length $110\pi/6$ ft?
- 37. In the figure, $\cot(\theta)$ is defined by what ratio?



38. What is the period of $y = \sin(-2x)$?

- 39. Simplify the expression $\left(\frac{\cot\theta\sec\theta}{\csc^2\theta}\right)$:
- 40. Simplify the expression $(\sec t \tan t)(\sec t + \tan t)$:

Self – Diagnostic Exam Solutions

$$1. \frac{x^4}{yz^8}$$

2.
$$\frac{m^{4x}}{m^{7y}}$$

3.
$$2(y^2 + 4x^2)(y - 2x)(y + 2x)$$

4.
$$\frac{x-3}{x^2+4x+3}$$
 or $\frac{x-3}{(x+1)(x+3)}$

$$5.-3(1+\sqrt{2})$$

$$6. \frac{2x}{y}$$

$$8. \frac{ab-1}{a-b}$$

$$9. \ \frac{40x+5}{60x-4}$$

10. There are no real solutions

11. 3 feet

12. 375 miles

13.
$$(x-2)^2 = 1$$

14.
$$y = 7x$$

15.
$$-\frac{1}{9}$$

16.
$$2xh + h^2$$

17.
$$\sqrt{x^2 - 6x}$$

18. All x less than 9

19.
$$y = -3x + 7$$

22.
$$\left(-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$$
 and $\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$

23. Vertex: (-3,12); maximum: 12

$$24. -\frac{17}{2} \le x \le \frac{3}{2}$$

25.
$$x \ge \frac{8}{3}$$
 or $x \le -\frac{4}{3}$

$$26. - 6 \le x \le 6$$

27. Roots: 3 and 4; each has multiplicity 2

$$28. - 0.25$$

30. The point is on the unit circle

31.
$$\frac{7\pi}{4}$$

34.
$$\sin(\theta)$$

35.
$$\frac{3}{4}$$

36.
$$\frac{11\pi}{6}$$

37.
$$\frac{x}{y}$$

38.
$$\pi$$

39.
$$sin(\theta)$$

Self-Diagnostic Test | Algebra and Trigonometry | ap-calc.github.io

Problems Numbered:	Topics Covered:
1-7	Basic concepts of Algebra
8-15	Equations, Inequalities, and Problem Solving
16-22	Functions and Graphs
23-27	Polynomial and Rational Functions
28-29	Exponential and Logarithmic Functions

30-40	Trigonometric Functions and Identities