

1) Find

$$\int_1^9 \frac{6}{\sqrt{x}} dx$$

- a) 108
  - b) 107
  - c) 36
  - d) 24
  - e) 12
- 2) If

$$f'(x) = -4(x-4)^2(x-9)$$

which of the following is true about  $y = f(x)$ ?

- a)  $f$  has a point of inflection at  $x = 4$  and a local maximum at  $x = 9$ .
  - b)  $f$  has a local maximum at  $x = 4$  and a local minimum at  $x = 9$ .
  - c)  $f$  has a local minimum at  $x = 4$  and a local maximum at  $x = 9$ .
  - d)  $f$  has a point of inflection at  $x = 4$  and a local minimum at  $x = 9$ .
  - e)  $f$  has a local minimum at  $x = 4$  and a point of inflection at  $x = 9$ .
- 3) A curve is described by parametric equations

$$[x = 4 \ln(t), y = t^2 - 6]$$

where  $t > 0$ . Give an expression for

$$\frac{\partial^2}{\partial x^2} y$$

- a)  $\frac{1}{4} t^2$
- b)  $t$
- c)  $\frac{1}{4} t$
- d)  $\frac{1}{2} t^2$
- e)  $\frac{1}{2} t$

4) Give the value for

$$\lim_{x \rightarrow 0} \left( \frac{1}{7} \frac{6^x - 1}{x} \right)$$

- a) *The limit does not exist.*
- b) 1
- c)  $7 \ln(6)$
- d)  $\frac{1}{7} \ln(6)$
- e) 0

5) Which of the following series converge?

I.

$$\sum_{n=1}^{\infty} \frac{\sin(n)}{n!}$$

II.

$$\sum_{n=1}^{\infty} \frac{x^{2n}}{n!}$$

III.

$$\sum_{n=1}^{\infty} \frac{1}{n(n+1)}$$

- a) I only  
 b) II and III only  
 c) I and II only  
 d) I, II and III  
 e) II only
- 6) If  $g(f(x)) = x$ ,  $g(6) = 2$  and  $g'(6) = 15$ , then  $f'(2)$  is

- a)  $\frac{1}{6}$   
 b)  $-\frac{1}{15}$   
 c)  $\frac{1}{15}$   
 d)  $-\frac{1}{6}$   
 e)  $\frac{2}{5}$

7) If  $f$  is a differentiable function and  $f(0) = -2$  and  $f(6) = 4$ , then which of the following must be true?

- I. There exists a  $c$  in  $[0,6]$  where  $f(c) = 0$ .  
 II. There exists a  $c$  in  $[0,6]$  where  $f'(c) = 0$ .  
 III. There exists a  $c$  in  $[0,6]$  where  $f'(c) = 1$ .

- a) I only  
 b) I and III only  
 c) II only  
 d) II and III only  
 e) I, II and III
- 8) Evaluate

$$\int_{-2}^2 \frac{6}{x^2} dx$$

- a)  $\frac{1}{2}$   
 b) 0  
 c) *The integral diverges.*

- d) 1  
 e)  $\frac{1}{4}$

9) Find the area enclosed by the graphs of

$$y = e^x + 1$$

$$y = 4$$

and the y-axis.

- a)  $8 \ln(2) - 4$   
 b)  $3 \ln(3) - 2$   
 c)  $8 \ln(2) + 4$   
 d)  $4 \ln(3) + 3$   
 e)  $4 \ln(3) - 3$

10) What is the minimum value of the function

$$f(x) = \frac{2}{\sqrt{x}} + 4\sqrt{x}$$

- a)  $\frac{1}{2}\sqrt{2}$   
 b)  $2\sqrt{2}$   
 c)  $\frac{1}{2}$   
 d)  $\sqrt{2}$   
 e)  $4\sqrt{2}$

11) Give the value of

$$\int_{\pi}^{2\pi} \frac{\cos(9x)}{2 + \sin(9x)} dx$$

- a)  $\frac{1}{9}$   
 b) 1  
 c) 0  
 d)  $\frac{1}{18}$   
 e)  $-\frac{1}{9}$

12) The side of a cube is expanding at a constant rate of 2 inches per second. What is the rate of change of the surface area, in  $\text{in}^2$  per second, when the volume of the cube is  $64 \text{ in}^3$ ?

- a) 48  
 b) 24  
 c) 96  
 d) 120  
 e) 12

13) Give the area inside one petal of the polar graph of

$$r = 7 \sin(2\theta)$$

- a)  $\frac{49}{8} \pi$
- b)  $\frac{49}{4} \pi$
- c)  $\frac{49}{2} \pi$
- d)  $\frac{49}{16} \pi$
- e)  $\frac{7}{2}$

14) Give the solution to the initial value problem

$$[y' = 15x^2 y, y(1) = 1]$$

- a)  $e^{5x^3}$
- b)  $e^{5x^3 - 5}$
- c)  $e^{5x^3} - 5$
- d)  $\frac{1}{5} \ln(x^3) + e$
- e)  $\frac{1}{5} \ln(x^3) + 1$

15) The position of a particle moving along a horizontal line is given by

$$x(t) = 2(t - 2)^3$$

What is the maximum speed of the particle for  $0 \leq t \leq 10$ ?

- a) 128
  - b) 384
  - c) 24
  - d) 48
  - e) 8
- 16)  $\int [\sec(4x)]^2 dx =$
- a)  $\frac{1}{4} \tan(4x) + C$
  - b)  $4 \tan(4x) + C$
  - c)  $-4 \tan(4x) + C$
  - d)  $4 [\tan(4x)]^2 + C$
  - e)  $\frac{1}{4} [\tan(4x)]^2 + C$

17) Define the function

$$f(x) = x e^{-5x}$$

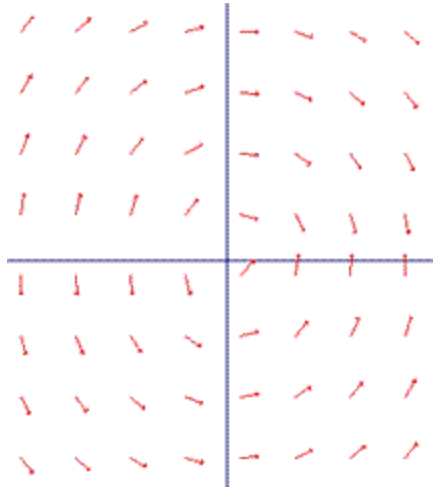
for  $x > 0$ . Give the interval on which the function is increasing.

- a)  $\left(0, \frac{1}{5} e\right)$
- b)  $(1, 5)$
- c)  $\left(1, \frac{1}{5} e\right)$

d)  $(0, 5)$

e)  $\left(0, \frac{1}{5}\right)$

18)



Which of the following differential equations correspond to the slope field shown in the figure above?

a)  $\frac{dy}{dx} = \frac{x}{y}$

b)  $\frac{dy}{dx} = \frac{y}{x}$

c)  $\frac{dy}{dx} = -\frac{y}{x}$

d)  $\frac{dy}{dx} = 4xy$

e)  $\frac{dy}{dx} = -\frac{x}{y}$

19) Evaluate

$$\lim_{h \rightarrow 0} \left( \frac{\cos(4x + 4h) - \cos(4x)}{h} \right)$$

a)  $-4 \cos(4x)$

b)  $4 \sin(4x)$

c)  $4 \cos(4x)$

d) *The limit does not exist.*

e)  $-4 \sin(4x)$

20) If  $\int_0^{64} e^x dx = m$  then  $\int_0^8 x e^{x^2} dx$  is

a)  $\frac{1}{2} m^2$

b)  $2m$

c)  $m^2$

d)  $\frac{1}{2} m$

e)  $m$

21) Find the area of the region enclosed by the graph of

and the line

$$y = 2x^2$$

$$y = 4x$$

- a)  $\frac{1}{6}$
- b)  $\frac{2}{3}$
- c)  $\frac{1}{12}$
- d)  $\frac{8}{3}$
- e)  $\frac{16}{3}$

22) Suppose

$$z = e^y$$
$$y = 6x^3 - 6$$

and

$$x = 1 + \ln(t^2)$$

What is  $dz/dt$  when  $t = 1$ ?

- a) 18
- b) 6
- c) 36
- d) 9
- e) 24

23) Evaluate

$$\int_0^{\frac{1}{2}\pi} \cos^2(9x) \sin(9x) \, dx$$

- a)  $\frac{1}{9}$
- b)  $\frac{1}{27}$
- c)  $\frac{1}{54}$
- d)  $-\frac{1}{27}$
- e)  $-\frac{1}{54}$

24) Give an equation for the tangent line to the parametric curve

$$[x = e^t, y = t^2 + 2t]$$

at  $t = 0$ .

- a)  $y = 2e(x-1)$
- b)  $y = \frac{2(x-1)}{e}$
- c)  $y = 2x - 2$

d)  $y - 1 = 2x$

e)  $y - 1 = 2x - 2$

25) Evaluate

$$\frac{\partial}{\partial x} \int_3^{6x} \ln(3t) dt$$

a)  $6 \ln(6x) - 12 \ln(3)$

b)  $3 \ln(18x)$

c)  $6 \ln(18x) - 12 \ln(3)$

d)  $6 \ln(18x)$

e)  $\frac{2}{x}$

26) The region bounded by

$$y = 5 \sin(x)$$

and the  $x$ -axis, for  $0 \leq x \leq \frac{1}{2}\pi$ , is rotated about the line  $y = -4$ . The volume of this solid can be represented

by:

a)  $2\pi \int_0^{\frac{1}{2}\pi} (5 \sin(x) + 4)^2 dx$

b)  $\pi \int_0^{\frac{1}{2}\pi} (25 \sin(x)^2 - 16) dx$

c)  $2\pi \int_0^{\frac{1}{2}\pi} 25 \sin(x + 4)^2 dx$

d)  $\pi \int_0^{\frac{1}{2}\pi} ((5 \sin(x) + 4)^2 - 16) dx$

e)  $2\pi \int_0^{\frac{1}{2}\pi} (25 \sin(x)^2 + 4) dx$

27) Give the third degree Taylor polynomial about  $x = 1$  of

$$f(x) = \ln(x)$$

a)  $(x-1) + \frac{1}{3}(x-1)^2 + \frac{1}{3}(x-1)^3$

b)  $(x-1) - \frac{1}{2}(x-1)^2 + \frac{1}{6}(x-1)^3$

c)  $(x-1) - \frac{1}{3}(x-1)^2 + \frac{1}{5}(x-1)^3$

d)  $(x-1) + (x-1)^2 + 2(x-1)^3$

e)  $(x-1) - \frac{1}{2}(x-1)^2 + \frac{1}{3}(x-1)^3$

28) Which of the following integrals gives the length of the graph of

$$f(x) = e^{2x}$$

for  $x$  between 0 and 2?

a)  $\int_0^2 \sqrt{x + e^{4x}} \, dx$

b)  $\int_0^2 \sqrt{1 + e^{4x}} \, dx$

c)  $\int_0^2 \sqrt{x + 4e^{4x}} \, dx$

d)  $\int_0^2 \sqrt{e^{2x} + 4e^{4x}} \, dx$

e)  $\int_0^2 \sqrt{1 + 4e^{4x}} \, dx$



29) Find the average value of the function

$$f(x) = e^{8x}$$

over the interval  $[0, 3]$ .

- a)  $\frac{1}{8} e^{24}$
- b)  $\frac{1}{24} e^{24}$
- c)  $\frac{1}{3} (e^{24} - 1)$
- d)  $\frac{1}{24} (e^{24} - 1)$
- e)  $\frac{1}{8} (e^{24} - 1)$

30) What is the y-intercept of the line tangent to the curve  $y = x^2 + 5$  at  $x = 3$ ?

- a)  $(0, -4)$
- b)  $(0, -1)$
- c)  $(0, -13)$
- d)  $(0, 13)$
- e)  $(0, 4)$

31) Which of the following function(s) is continuous and differentiable?

I.  $f(x) = \frac{5}{\sqrt{x}}$

II.  $g(x) = x|x|$

III.  $h(x) = \begin{cases} 8x + 1 & x \leq 0 \\ x^2 + 1 & 0 < x \end{cases}$

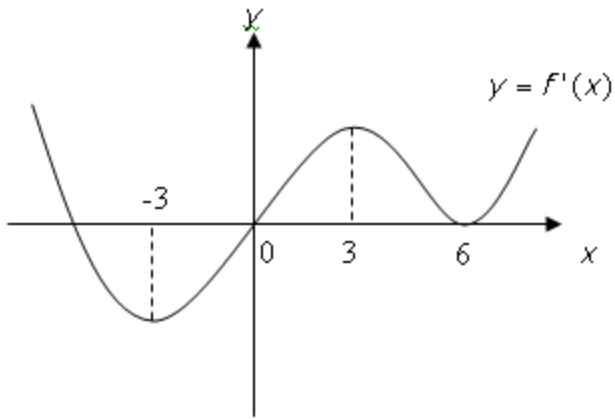
- a) I only
- b) II only
- c) III only
- d) I and II only
- e) I and III only

32) Find  $m$

$$\lim_{x \rightarrow 0} \left( \frac{e^{mx^2} - \cos(10x)}{x^2} \right) = 100$$

- a)  $\frac{5}{2}$
- b) 5
- c) 25
- d) 50
- e) 200

33) The graph of the derivative of  $f$  is shown below. Which of the following must be true?



- a)  $f$  has a local minimum at  $x = -3$ .  
 b)  $f$  has a local maximum at  $x = 0$ .  
 c)  $f$  is concave down on  $[0, 6]$ .  
 d)  $f$  has a point of inflection at  $x = 6$ .  
 e)  $f$  is increasing on  $[-3, 3]$ .

34) The sum of two positive integers  $x$  and  $y$  is 150. Find the value of  $x$  that minimizes

$$P = x^3 - 150xy$$

- a)  $x = 25$   
 b)  $x = 75$   
 c)  $x = 50$   
 d)  $x = 125$   
 e)  $x = 100$

35) A particle moves on the curve

$$[x = 8 \sin(t), y = \sin(2t)]$$

find the speed of the particle at time  $t = \pi$ .

- a) 7.7460  
 b) 8.2462  
 c) 8.1240  
 d) 3.4641  
 e) 3.1623

36) The function  $f$  is defined as

$$f(x) = \frac{(x-2)^2}{x-6}$$

$$x \neq 6$$

Which of the following is **false**?

- a)  $f$  is decreasing on  $[2, 6]$ .  
 b)  $f$  has a vertical asymptote at  $x = 6$ .  
 c)  $f$  has a horizontal asymptote at  $y = 1$ .  
 d)  $f$  has a local maximum at  $x = 2$ .  
 e)  $f$  is concave up for  $x > 6$ .

37) A particle is moving along the  $x$ -axis and its position at time  $t \geq 0$  is given by

$$S(t) = (t-4)^2(t-5)$$

Which of the following is (are) true?

- I. The particle changes direction at  $x = 4$  and  $x = 5$ .

II. The particle is slowing down on  $[0, 4]$ .

III. The particle is speeding up on  $[4, 5]$ .

- a) I only
- b) II only
- c) II and III only
- d) I and III only
- e) I, II and III

38)  $f(x)$  is a differentiable function and it is decreasing on  $(-\infty, \infty)$ .

If

$$g(x) = f(6x^3 - x^2)$$

then  $g$  has a local maximum at

- a)  $x = 3$
- b)  $x = 0$
- c)  $x = 1$
- d)  $x = \frac{1}{3}$
- e)  $x = \frac{1}{9}$

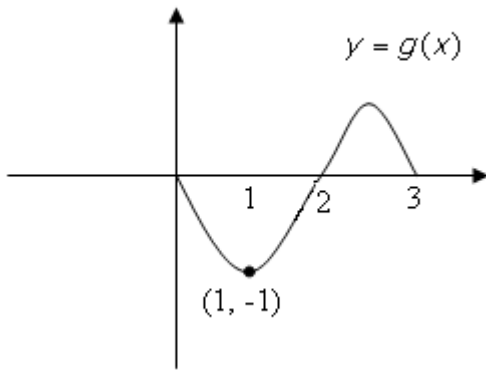
39) The rate at which a bacteria population grows is proportional to the number of bacteria present. Initially, there were 1000 bacteria present and the population doubled in 4 hours. Roughly how many hours does it take for the population to reach 10000?

- a) 20.8
- b) 16.4
- c) 13.2
- d) 8.8
- e) 11.6

40) Find the radius of convergence of the series

$$\sum_{n=1}^{\infty} \frac{n(7x-11)^n}{2^n}$$

- a)  $\frac{2}{11}$
- b)  $\frac{7}{2}$
- c)  $\frac{2}{7}$
- d)  $\frac{11}{7}$
- e)  $\frac{11}{2}$



41)

$$g(x) = \int_0^x f(t) dt$$

for  $0 \leq x \leq 3$

The graph of  $g$  is shown above. Which of the following must be true?

- I.  $\int_0^3 f(t) dt = 0$
- II.  $\int_1^2 f(t) dt = 1$
- III.  $\int_2^0 f(t) dt = -1$

- a) I and II only
- b) I only
- c) II only
- d) I and III only
- e) II and III only

42) If the region bounded by  $y = \tan^{-1}(x)$ ,  $y = \frac{1}{4} \pi$  and the y-axis is rotated about the y-axis, the volume of

the solid formed is

- a) 0.215
- b) 0.674
- c) 1.348
- d) 0.430
- e) 0.413

43)  $f(x)$  is represented by the Maclaurin series

$$1 - \frac{(2x)^2}{2!} + \frac{(2x)^4}{4!} - \dots + (-1)^n \frac{(2x)^{2n}}{(2n)!} + \dots$$

What is the slope of the line normal to the graph of  $f$  at  $x = \frac{7}{4} \pi$ ?

- a)  $\frac{1}{2}$
- b)  $-\frac{1}{2}$
- c) 0
- d) 2

e)  $-2$

44) What are all values of  $h$  for which

$$\int_0^{\infty} \frac{6x}{(x^2 + 1)^h} dx$$

converge?

a)  $h > 1$

b)  $h < 1$

c)  $h \geq 1$

d)  $h \leq 1$

e)  $-1 < h < 1$

45) The base of a solid is the region bounded by

$$y = 8\sqrt{x}$$

the  $x$ -axis, and

the line  $x = 8$

Each cross-section of the solid perpendicular to the  $x$ -axis is a square, with one side on the  $xy$ -plane. Which of the following expressions represents the volume of the solid?

a)  $\int_0^1 64x \, dx$

b)  $\int_0^8 8\sqrt{x} \, dx$

c)  $\int_0^8 8x \, dx$

d)  $\int_0^1 8\sqrt{x} \, dx$

e)  $\int_0^8 64x \, dx$

1) Find

$$\int_1^9 \frac{6}{\sqrt{x}} dx$$

- a) 108
  - b) 107
  - c) 36
  - \*d) 24
  - e) 12
- 2) If

$$f'(x) = -4(x-4)^2(x-9)$$

which of the following is true about  $y = f(x)$ ?

- \*a)  $f$  has a point of inflection at  $x = 4$  and a local maximum at  $x = 9$ .
  - b)  $f$  has a local maximum at  $x = 4$  and a local minimum at  $x = 9$ .
  - c)  $f$  has a local minimum at  $x = 4$  and a local maximum at  $x = 9$ .
  - d)  $f$  has a point of inflection at  $x = 4$  and a local minimum at  $x = 9$ .
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- b)  $t$
- c)  $\frac{1}{4} t$
- d)  $\frac{1}{2} t^2$
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4) Give the value for

$$\lim_{x \rightarrow 0} \left( \frac{1}{7} \frac{6^x - 1}{x} \right)$$

- a) *The limit does not exist.*
- b) 1
- c)  $7 \ln(6)$
- \*d)  $\frac{1}{7} \ln(6)$
- e) 0

5) Which of the following series converge?

I.

$$\sum_{n=1}^{\infty} \frac{\sin(n)}{n!}$$

II.

$$\sum_{n=1}^{\infty} \frac{x^{2n}}{n!}$$

III.

$$\sum_{n=1}^{\infty} \frac{1}{n(n+1)}$$

- a) I only  
 b) II and III only  
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 e)  $\frac{2}{5}$

7) If  $f$  is a differentiable function and  $f(0) = -2$  and  $f(6) = 4$ , then which of the following must be true?

- I. There exists a  $c$  in  $[0,6]$  where  $f(c) = 0$ .  
 II. There exists a  $c$  in  $[0,6]$  where  $f'(c) = 0$ .  
 III. There exists a  $c$  in  $[0,6]$  where  $f'(c) = 1$ .

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 \*b) I and III only  
 c) II only  
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$$\int_{-2}^2 \frac{6}{x^2} dx$$

- a)  $\frac{1}{2}$   
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- d) 1  
 e)  $\frac{1}{4}$

9) Find the area enclosed by the graphs of

$$y = e^x + 1$$

$$y = 4$$

and the y-axis.

- a)  $8 \ln(2) - 4$   
 \*b)  $3 \ln(3) - 2$   
 c)  $8 \ln(2) + 4$   
 d)  $4 \ln(3) + 3$   
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10) What is the minimum value of the function

$$f(x) = \frac{2}{\sqrt{x}} + 4\sqrt{x}$$

- a)  $\frac{1}{2}\sqrt{2}$   
 b)  $2\sqrt{2}$   
 c)  $\frac{1}{2}$   
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$$\int_{\pi}^{2\pi} \frac{\cos(9x)}{2 + \sin(9x)} dx$$

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12) The side of a cube is expanding at a constant rate of 2 inches per second. What is the rate of change of the surface area, in  $\text{in}^2$  per second, when the volume of the cube is  $64 \text{ in}^3$ ?

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b)  $\frac{49}{4} \pi$

c)  $\frac{49}{2} \pi$

d)  $\frac{49}{16} \pi$

e)  $\frac{7}{2}$

14) Give the solution to the initial value problem

$$[y' = 15x^2 y, y(1) = 1]$$

a)  $e^{5x^3}$

\*b)  $e^{5x^3 - 5}$

c)  $e^{5x^3} - 5$

d)  $\frac{1}{5} \ln(x^3) + e$

e)  $\frac{1}{5} \ln(x^3) + 1$

15) The position of a particle moving along a horizontal line is given by

$$x(t) = 2(t-2)^3$$

What is the maximum speed of the particle for  $0 \leq t \leq 10$ ?

a) 128

\*b) 384

c) 24

d) 48

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\*a)  $\frac{1}{4} \tan(4x) + C$

b)  $4 \tan(4x) + C$

c)  $-4 \tan(4x) + C$

d)  $4 [\tan(4x)]^2 + C$

e)  $\frac{1}{4} [\tan(4x)]^2 + C$

17) Define the function

$$f(x) = x e^{-5x}$$

for  $x > 0$ . Give the interval on which the function is increasing.

a)  $\left(0, \frac{1}{5} e\right)$

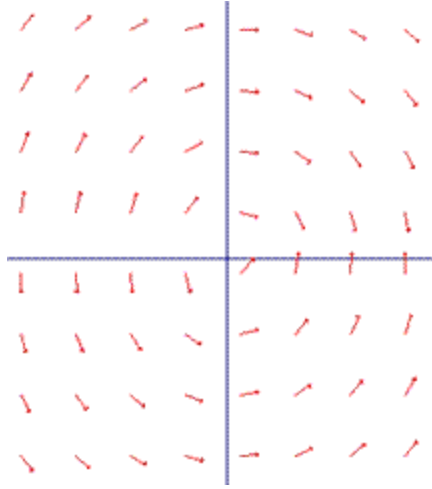
b)  $(1, 5)$

c)  $\left(1, \frac{1}{5} e\right)$

d)  $(0, 5)$

\*e)  $\left(0, \frac{1}{5}\right)$

18)



Which of the following differential equations correspond to the slope field shown in the figure above?

a)  $\frac{dy}{dx} = \frac{x}{y}$

b)  $\frac{dy}{dx} = \frac{y}{x}$

c)  $\frac{dy}{dx} = -\frac{y}{x}$

d)  $\frac{dy}{dx} = 4xy$

\*e)  $\frac{dy}{dx} = -\frac{x}{y}$

19) Evaluate

$$\lim_{h \rightarrow 0} \left( \frac{\cos(4x + 4h) - \cos(4x)}{h} \right)$$

a)  $-4 \cos(4x)$

b)  $4 \sin(4x)$

c)  $4 \cos(4x)$

d) *The limit does not exist.*

\*e)  $-4 \sin(4x)$

20) If  $\int_0^{64} e^x dx = m$  then  $\int_0^8 x e^{x^2} dx$  is

a)  $\frac{1}{2} m^2$

b)  $2m$

c)  $m^2$

\*d)  $\frac{1}{2} m$

e)  $m$

21) Find the area of the region enclosed by the graph of

and the line

$$y = 2x^2$$

$$y = 4x$$

- a)  $\frac{1}{6}$
- b)  $\frac{2}{3}$
- c)  $\frac{1}{12}$
- \*d)  $\frac{8}{3}$
- e)  $\frac{16}{3}$

22) Suppose

$$z = e^y$$
$$y = 6x^3 - 6$$

and

$$x = 1 + \ln(t^2)$$

What is  $dz/dt$  when  $t = 1$ ?

- a) 18
- b) 6
- \*c) 36
- d) 9
- e) 24

23) Evaluate

$$\int_0^{\frac{1}{2}\pi} \cos^2(9x) \sin(9x) dx$$

- a)  $\frac{1}{9}$
- \*b)  $\frac{1}{27}$
- c)  $\frac{1}{54}$
- d)  $-\frac{1}{27}$
- e)  $-\frac{1}{54}$

24) Give an equation for the tangent line to the parametric curve

$$[x = e^t, y = t^2 + 2t]$$

at  $t = 0$ .

- a)  $y = 2e(x-1)$
- b)  $y = \frac{2(x-1)}{e}$
- \*c)  $y = 2x - 2$

d)  $y - 1 = 2x$

e)  $y - 1 = 2x - 2$

25) Evaluate

$$\frac{\partial}{\partial x} \int_3^{6x} \ln(3t) dt$$

a)  $6 \ln(6x) - 12 \ln(3)$

b)  $3 \ln(18x)$

c)  $6 \ln(18x) - 12 \ln(3)$

\*d)  $6 \ln(18x)$

e)  $\frac{2}{x}$

26) The region bounded by

$$y = 5 \sin(x)$$

and the  $x$ -axis, for  $0 \leq x \leq \frac{1}{2}\pi$ , is rotated about the line  $y = -4$ . The volume of this solid can be represented

by:

a)  $2\pi \int_0^{\frac{1}{2}\pi} (5 \sin(x) + 4)^2 dx$

b)  $\pi \int_0^{\frac{1}{2}\pi} (25 \sin(x)^2 - 16) dx$

c)  $2\pi \int_0^{\frac{1}{2}\pi} 25 \sin(x + 4)^2 dx$

\*d)  $\pi \int_0^{\frac{1}{2}\pi} ((5 \sin(x) + 4)^2 - 16) dx$

e)  $2\pi \int_0^{\frac{1}{2}\pi} (25 \sin(x)^2 + 4) dx$

27) Give the third degree Taylor polynomial about  $x = 1$  of

$$f(x) = \ln(x)$$

a)  $(x-1) + \frac{1}{3}(x-1)^2 + \frac{1}{3}(x-1)^3$

b)  $(x-1) - \frac{1}{2}(x-1)^2 + \frac{1}{6}(x-1)^3$

c)  $(x-1) - \frac{1}{3}(x-1)^2 + \frac{1}{5}(x-1)^3$

d)  $(x-1) + (x-1)^2 + 2(x-1)^3$

\*e)  $(x-1) - \frac{1}{2}(x-1)^2 + \frac{1}{3}(x-1)^3$

28) Which of the following integrals gives the length of the graph of

$$f(x) = e^{2x}$$

for  $x$  between 0 and 2?

a)  $\int_0^2 \sqrt{x + e^{4x}} \, dx$

b)  $\int_0^2 \sqrt{1 + e^{4x}} \, dx$

c)  $\int_0^2 \sqrt{x + 4e^{4x}} \, dx$

d)  $\int_0^2 \sqrt{e^{2x} + 4e^{4x}} \, dx$

\*e)  $\int_0^2 \sqrt{1 + 4e^{4x}} \, dx$

29) Find the average value of the function

$$f(x) = e^{8x}$$

over the interval  $[0, 3]$ .

a)  $\frac{1}{8} e^{24}$

b)  $\frac{1}{24} e^{24}$

c)  $\frac{1}{3} (e^{24} - 1)$

\*d)  $\frac{1}{24} (e^{24} - 1)$

e)  $\frac{1}{8} (e^{24} - 1)$

30) What is the y-intercept of the line tangent to the curve  $y = x^2 + 5$  at  $x = 3$ ?

\*a)  $(0, -4)$

b)  $(0, -1)$

c)  $(0, -13)$

d)  $(0, 13)$

e)  $(0, 4)$

31) Which of the following function(s) is continuous and differentiable?

I.  $f(x) = \frac{5}{\sqrt{x}}$

II.  $g(x) = x|x|$

III.  $h(x) = \begin{cases} 8x + 1 & x \leq 0 \\ x^2 + 1 & 0 < x \end{cases}$

\*a) I only

b) II only

c) III only

d) I and II only

e) I and III only

32) Find  $m$

$$\lim_{x \rightarrow 0} \left( \frac{e^{mx^2} - \cos(10x)}{x^2} \right) = 100$$

a)  $\frac{5}{2}$

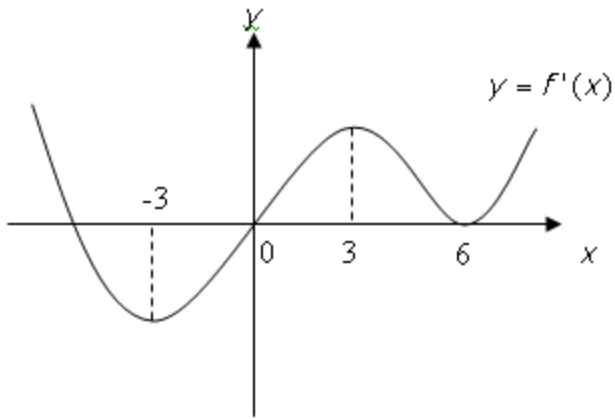
b) 5

c) 25

\*d) 50

e) 200

33) The graph of the derivative of  $f$  is shown below. Which of the following must be true?



- a)  $f$  has a local minimum at  $x = -3$ .
- b)  $f$  has a local maximum at  $x = 0$ .
- c)  $f$  is concave down on  $[0, 6]$ .
- \*d)  $f$  has a point of inflection at  $x = 6$ .
- e)  $f$  is increasing on  $[-3, 3]$ .

34) The sum of two positive integers  $x$  and  $y$  is 150. Find the value of  $x$  that minimizes

$$P = x^3 - 150xy$$

- a)  $x = 25$
- b)  $x = 75$
- \*c)  $x = 50$
- d)  $x = 125$
- e)  $x = 100$

35) A particle moves on the curve

$$[x = 8 \sin(t), y = \sin(2t)]$$

find the speed of the particle at time  $t = \pi$ .

- a) 7.7460
- \*b) 8.2462
- c) 8.1240
- d) 3.4641
- e) 3.1623

36) The function  $f$  is defined as

$$f(x) = \frac{(x-2)^2}{x-6}$$

$$x \neq 6$$

Which of the following is **false**?

- a)  $f$  is decreasing on  $[2, 6]$ .
- b)  $f$  has a vertical asymptote at  $x = 6$ .
- \*c)  $f$  has a horizontal asymptote at  $y = 1$ .
- d)  $f$  has a local maximum at  $x = 2$ .
- e)  $f$  is concave up for  $x > 6$ .

37) A particle is moving along the  $x$ -axis and its position at time  $t \geq 0$  is given by

$$S(t) = (t-4)^2(t-5)$$

Which of the following is (are) true?

- I. The particle changes direction at  $x = 4$  and  $x = 5$ .

II. The particle is slowing down on  $[0, 4]$ .

III. The particle is speeding up on  $[4, 5]$ .

a) I only

\*b) II only

c) II and III only

d) I and III only

e) I, II and III

38)  $f(x)$  is a differentiable function and it is decreasing on  $(-\infty, \infty)$ .

If

$$g(x) = f(6x^3 - x^2)$$

then  $g$  has a local maximum at

a)  $x = 3$

b)  $x = 0$

c)  $x = 1$

d)  $x = \frac{1}{3}$

\*e)  $x = \frac{1}{9}$

39) The rate at which a bacteria population grows is proportional to the number of bacteria present. Initially, there were 1000 bacteria present and the population doubled in 4 hours. Roughly how many hours does it take for the population to reach 10000?

a) 20.8

b) 16.4

\*c) 13.2

d) 8.8

e) 11.6

40) Find the radius of convergence of the series

$$\sum_{n=1}^{\infty} \frac{n(7x-11)^n}{2^n}$$

a)  $\frac{2}{11}$

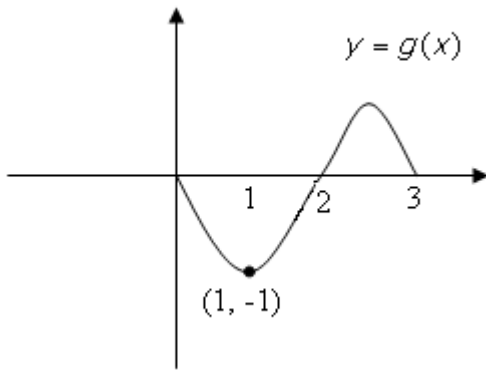
b)  $\frac{7}{2}$

\*c)  $\frac{2}{7}$

d)  $\frac{11}{7}$

e)  $\frac{11}{2}$





41)

$$g(x) = \int_0^x f(t) dt$$

for  $0 \leq x \leq 3$

The graph of  $g$  is shown above. Which of the following must be true?

- I.  $\int_0^3 f(t) dt = 0$
- II.  $\int_1^2 f(t) dt = 1$
- III.  $\int_2^0 f(t) dt = -1$

- \*a) I and II only
- b) I only
- c) II only
- d) I and III only
- e) II and III only

42) If the region bounded by  $y = \tan^{-1}(x)$ ,  $y = \frac{1}{4} \pi$  and the y-axis is rotated about the y-axis, the volume of

the solid formed is

- a) 0.215
- \*b) 0.674
- c) 1.348
- d) 0.430
- e) 0.413

43)  $f(x)$  is represented by the Maclaurin series

$$1 - \frac{(2x)^2}{2!} + \frac{(2x)^4}{4!} - \dots + (-1)^n \frac{(2x)^{2n}}{(2n)!} + \dots$$

What is the slope of the line normal to the graph of  $f$  at  $x = \frac{7}{4} \pi$ ?

- a)  $\frac{1}{2}$
- \*b)  $-\frac{1}{2}$
- c) 0
- d) 2

e)  $-2$

44) What are all values of  $h$  for which

$$\int_0^{\infty} \frac{6x}{(x^2 + 1)^h} dx$$

converge?

\*a)  $h > 1$

b)  $h < 1$

c)  $h \geq 1$

d)  $h \leq 1$

e)  $-1 < h < 1$

45) The base of a solid is the region bounded by

$$y = 8\sqrt{x}$$

the  $x$ -axis, and

the line  $x = 8$

Each cross-section of the solid perpendicular to the  $x$ -axis is a square, with one side on the  $xy$ -plane. Which of the following expressions represents the volume of the solid?

a)  $\int_0^1 64x \, dx$

b)  $\int_0^8 8\sqrt{x} \, dx$

c)  $\int_0^8 8x \, dx$

d)  $\int_0^1 8\sqrt{x} \, dx$

\*e)  $\int_0^8 64x \, dx$