

1) Find

$$\lim_{h \rightarrow 0} \left( \frac{\sin(4x + 4h) - \sin(4x)}{h} \right)$$

- a)  $-4 \sin(4x)$
- b)  $0$
- c)  $-4 \cos(4x)$
- d)  $4 \cos(4x)$
- e)  $4 \sin(4x)$

2) The function  $g$  is defined by the formula

$$g(x) = \int_0^x e^{3t} dt$$

Find the slope of the tangent line at  $x = 1$ .

- a)  $e^3$
- b)  $3e^3$
- c)  $\frac{1}{3}e^3$
- d)  $\frac{1}{3}(e^3 - 1)$
- e)  $e^3 - 1$

3) Find

$$\lim_{x \rightarrow \infty} \left( \frac{3x - 1}{\sqrt{x^2 + 9}} \right)$$

- a)  $3$
- b)  $\frac{1}{3}$
- c)  $1$
- d)  $-\frac{1}{9}$

e) The limit does not exist.

4) The given function  $f$  has a removable discontinuity at  $x = -5$ . Find  $A$ .

$$f(x) = \begin{cases} 5x^2 + 8 & x < -5 \\ 8x & x = -5 \\ Ax + 8 & -5 < x \end{cases}$$

- a)  $-4$
- b)  $5$
- c)  $-15$
- d)  $-25$
- e)  $-5$

5) If  $f'(x) = -5(x-4)^2(x-8)$  which of the following is true about  $y = f(x)$ ?

- a)  $f$  has a local minimum at  $x = 4$  and a point of inflection at  $x = 8$ .
- b)  $f$  has a local minimum at  $x = 4$  and a local maximum at  $x = 8$ .
- c)  $f$  has a point of inflection at  $x = 4$  and a local minimum at  $x = 8$ .
- d)  $f$  has a point of inflection at  $x = 4$  and a local maximum at  $x = 8$ .
- e)  $f$  has a local maximum at  $x = 4$  and a local minimum at  $x = 8$ .

6) Find  $f'(9)$ , given that

$$f(x) = 2x^2 + 5\sqrt{x}$$

- a) 177
- b) 207
- c)  $\frac{221}{6}$
- d) 51
- e)  $\frac{113}{3}$

7) Find the average value of the given function  $f$  over the interval  $[0, 3]$ .

$$f(x) = e^{7x}$$

- a)  $\frac{1}{7}(e^{21} - 1)$
- b)  $\frac{1}{21}(e^{21} - 1)$
- c)  $\frac{1}{21}e^{21}$
- d)  $\frac{1}{3}(e^{21} - 1)$
- e)  $\frac{1}{7}e^{21}$

8) Find  $f'(0)$ , given that

$$f(x) = 2^x \ln(5e^x)$$

- a)  $\ln(5) + 1$
- b) 1
- c)  $\ln(2) \ln(5) + 1$
- d)  $\ln(2) \ln(5) + 2$
- e)  $\ln(10) + 1$

9) Find  $f'(1)$ , given that

$$f(x) = \frac{x^2 + 7}{(8x)}$$

- a)  $\frac{15}{64}$
- b)  $-\frac{3}{4}$
- c)  $\frac{1}{64}$
- d)  $\frac{15}{8}$
- e)  $\frac{7}{4}$

10) Find

$$\lim_{x \rightarrow 0} \left( \frac{\sin(8x) \cos(x) - \sin(x) \cos(8x)}{x^2} \right)$$

- a) 1
- b) 8
- c) -8
- d) The limit does not exist.
- e) 0

11) Given the following curve, find  $\frac{d^2y}{dx^2}$ .

$$7x + y^2 = 15$$

a)  $-\frac{7}{2y^2}$

b)  $\frac{7}{2y^2}$

c)  $-\frac{49}{4y^3}$

d)  $\frac{49}{4y^3}$

e)  $\frac{49}{2y^3}$

12) Given that  $f(x) = 6\sin^2(3x)$ , find  $f''\left(\frac{1}{18}\pi\right)$ .

a)  $18\sqrt{2}$

b) 0

c) 54

d) 18

e)  $18\sqrt{3}$

13) Find the midpoint rectangular approximation for  $\int_0^3 2x^3 dx$  using 3 subintervals of equal length.

a)  $\frac{153}{4}$

b) 72

c)  $\frac{153}{2}$

d) 144

e)  $\frac{25}{4}$

14) Find the derivative of the function  $y = \cos^{-1}(5x)$ .

a)  $\frac{5}{\sqrt{1+25x^2}}$

b)  $-\frac{5}{\sqrt{1-25x^2}}$

c)  $-5\sin(5x)$

d)  $5\sin(5x)$

e)  $-5\sin^{-1}(5x)$

15) Find

$$\frac{\partial}{\partial x} \left( \int_2^x \ln(4+t) dt \right)$$

a)  $-\ln(4+x)$

b)  $\ln(4+x)$

c)  $2 \ln(4 + x)$

d)  $\frac{1}{4 + x}$

e)  $\frac{2}{4 + x}$

16) Find the equation of the tangent line to the given curve at the point (0, 7).

$$y = 5x^2 + 10x + 7$$

a)  $y = 10x + 7$

b)  $y = 10x - 7$

c)  $y = 7x + 5$

d)  $y = -5x + 7$

e)  $y = 20x$

17) If  $g(f(x)) = x$ ,  $g(4) = 2$  and  $g'(4) = 12$ , then  $f'(2)$  is

a)  $-\frac{1}{4}$

b)  $-\frac{1}{12}$

c)  $\frac{1}{4}$

d)  $\frac{1}{3}$

e)  $\frac{1}{12}$

18) Given that  $\int_0^{36} e^x dx = m$

find  $\int_0^6 x e^{x^2} dx$

a)  $m^2$

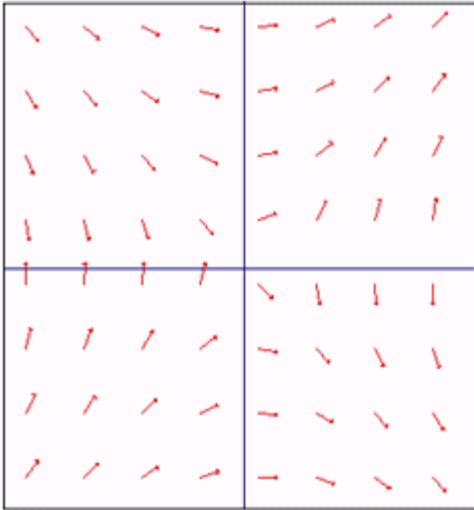
b)  $m$

c)  $2m$

d)  $\frac{1}{2} m^2$

e)  $\frac{1}{2} m$

19) Which of the following differential equations corresponds to the slope field shown in the figure below?



- a)  $\frac{dy}{dx} = -\frac{y}{x}$   
 b)  $\frac{dy}{dx} = \frac{1}{5}xy$   
 c)  $\frac{dy}{dx} = \frac{1}{10}xy$   
 d)  $\frac{dy}{dx} = \frac{y}{x}$   
 e)  $\frac{dy}{dx} = \frac{x}{y}$

20) Given the following function, with  $x > 0$ , on which interval is the function decreasing?

$$f(x) = \frac{x}{\ln(7x)}$$

- a)  $\left(1, \frac{1}{7}e\right)$   
 b)  $\left(0, \frac{1}{7}\right)$   
 c)  $(1, 7)$   
 d)  $\left(0, \frac{1}{7}e\right)$   
 e)  $(1, 7e)$

21) Find the area of the region enclosed by the graphs of

$$y = 3x^2$$

and

$$y = 2x$$

- a)  $\frac{9}{4}$   
 b)  $\frac{2}{27}$   
 c)  $\frac{9}{8}$   
 d)  $\frac{4}{27}$   
 e)  $\frac{8}{27}$

22) Find

$$\int_1^4 \frac{5}{\sqrt{x}} dx$$

- a) 39
- b) 5
- c) 10
- d) 20
- e) 40

23) The region bounded by the following graph

$$y = 2 \sin(x)$$

and the  $x$ -axis, for  $0 \leq x \leq \frac{1}{2} \pi$ , is rotated about the line  $y = -3$ . The volume of this solid can be represented

by:

a)  $2 \pi \int_0^{\frac{1}{2} \pi} (4 \sin(x)^2 + 3) dx$

b)  $\pi \int_0^{\frac{1}{2} \pi} ((2 \sin(x) + 3)^2 - 9) dx$

c)  $\pi \int_0^{\frac{1}{2} \pi} (4 \sin(x)^2 - 9) dx$

d)  $2 \pi \int_0^{\frac{1}{2} \pi} 4 \sin(3 + x)^2 dx$

e)  $2 \pi \int_0^{\frac{1}{2} \pi} (2 \sin(x) + 3)^2 dx$

24) The side of a cube is expanding at a constant rate of 5 inches per second. What is the rate of change of the volume, in  $in^3$  per second, when the total surface area of the cube is  $54 in^2$ ?

- a) 90
- b) 45
- c) 135
- d) 15
- e) 270

25) The solution to the differential equation

$$\frac{dy}{dx} = 4xy$$

with the initial condition  $y(0) = 6$  is

- a)  $6 \ln(2x^2)$
- b)  $e^{2x^2} + 5$
- c)  $\ln(2x^2 + 6)$

d)  $6 e^{2x^2}$

e)  $e^{2x^2} + 6$

26)  $\int \sec^2(6x) dx =$

a)  $\frac{1}{6} \tan^2(6x) + C$

b)  $-6 \tan(6x) + C$

c)  $6 \tan^2(6x) + C$

d)  $\frac{1}{6} \tan(6x) + C$

e)  $6 \tan(6x) + C$

27) The position of a particle moving along a horizontal line is given by

$$x(t) = 2(t-4)^3$$

What is the maximum speed of the particle for  $0 \leq t \leq 10$ ?

a) 384

b) 72

c) 96

d) 32

e) 216

28) Using the information below, find  $\frac{dz}{dt}$  when  $t = 0$ .

$$\begin{aligned}z &= \ln(y) \\y &= 4x^2 + 4 \\x &= 2t + 1\end{aligned}$$

a)  $\frac{1}{4}$

b) 8

c) 16

d)  $\frac{1}{2}$

e) 2

29) If  $f$  is a differentiable function and  $f(0) = -3$  and  $f(5) = 6$ , then which of the following must be true?

- I. There exists a  $c$  in  $[0,5]$  where  $f(c) = 0$ .
- II. There exists a  $c$  in  $[0,5]$  where  $f'(c) = 0$ .
- III. There exists a  $c$  in  $[0,5]$  where  $f'(c) = 9/5$ .

- a) I, II and III
- b) II only
- c) II and III only
- d) I and III only
- e) I only

30) Which of the following function(s) is continuous and differentiable?

I.  $f(x) = \frac{8}{\sqrt{x}}$

II.  $g(x) = x|x|$

III.  $h(x) = \begin{cases} 6x + 1 & x \leq 0 \\ x^2 + 1 & 0 < x \end{cases}$

- a) I only
- b) II only
- c) III only
- d) I and II only
- e) I and III only

31) The area of the region in the first quadrant bounded by the graphs of  $y = 3\cos(x)$ ,  $y = 3\sin(x)$ , and the  $y$ -axis is

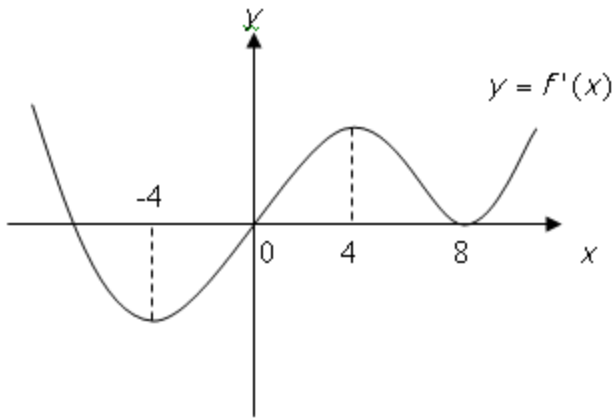
- a)  $3(\sqrt{2} - 1)$
- b)  $\frac{3}{2}\sqrt{2}$
- c) 6
- d)  $3\sqrt{2} + 1$
- e)  $3\sqrt{2}$

32) Air is pumped into a spherical balloon at a rate of  $9\text{cm}^3$  per second. At what rate is the radius of the sphere changing when its volume is  $36\pi\text{cm}^3$ ? 

- a)  $\frac{1}{8\pi}$  cm/sec
- b)  $\frac{3}{8\pi}$  cm/sec
- c)  $\frac{1}{\pi}$  cm/sec
- d)  $\frac{1}{4\pi}$  cm/sec
- e)  $\frac{3}{\pi}$  cm/sec

33) The graph of the derivative of  $f$  is shown below. Which of the following must be true?





- a)  $f$  has a local minimum at  $x = -4$ .
- b)  $f$  has a local maximum at  $x = 0$ .
- c)  $f$  is concave down on  $[0, 8]$ .
- d)  $f$  has a point of inflection at  $x = 8$ .
- e)  $f$  is increasing on  $[-4, 4]$ .

34) A particle is moving along the  $x$ -axis and its position at time  $t \geq 0$  is given by

$$S(t) = (t - 3)^2 (t - 6)$$

Which of the following is (are) true?

- I. The particle changes direction at  $x = 3$  and  $x = 6$ .
  - II. The particle is slowing down on  $[0, 3]$ .
  - III. The particle is speeding up on  $[3, 6]$ .
- a) II and III only
  - b) I only
  - c) II only
  - d) I and III only
  - e) I, II and III

35) The region enclosed by the graphs of

$$y = 5e^x$$

and the line

$$y = 5$$

for  $0 \leq x \leq 1$ , is revolved about the  $y$ -axis. Which of the following integrals gives the volume generated?

- a)  $\pi \int_0^1 (5e^x - 5)^2 dx$
- b)  $\pi \int_5^{5e} \left( 1 - \left( \ln\left(\frac{1}{5}y\right) \right)^2 \right) dy$
- c)  $\pi \int_5^{5e} \left( 5 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$
- d)  $\pi \int_0^5 \left( 1 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$
- e)  $\pi \int_5^{5e} \left( 1 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$

36) If

$$4x^2 + xy - \cos(y) = 10$$

then  $\frac{dy}{dx}$  is

- a)  $-\frac{8x}{x + \sin(y)}$
- b)  $\frac{y - 8x}{x - \sin(y)}$
- c)  $-\frac{(y + 8x)}{x + \sin(y)}$
- d)  $\frac{y + x}{x - \sin(y)}$
- e)  $-\frac{(x + \sin(y))}{y + 8x}$

37) The sum of two positive integers  $x$  and  $y$  is 60. Find the value of  $x$  that minimizes

$$P = x^3 - 60xy$$

- a)  $x = 30$
- b)  $x = 20$
- c)  $x = 10$
- d)  $x = 50$
- e)  $x = 40$

38) A particle moves along a straight line, and its velocity at time  $t$  is given by

$$v(t) = 4 - \ln(t)$$

What is the total distance the particle travels from  $t = 1$  to  $t = e$ ?

- a)  $4e + 4$
- b)  $4e - 1$
- c)  $4e + 1$
- d)  $e - 5$
- e)  $4e - 5$

39) The function  $f$  is defined as

$$f(x) = \frac{(x-5)^2}{x-6}$$

$$x \neq 6$$

Which of the following is **false**?

- a)  $f$  is decreasing on  $[5, 6]$ .
- b)  $f$  has a vertical asymptote at  $x = 6$ .
- c)  $f$  has a horizontal asymptote at  $y = 1$ .
- d)  $f$  has a local maximum at  $x = 5$ .
- e)  $f$  is concave up for  $x > 6$ .

40) The base of a solid is the region bounded by

$$y = 5\sqrt{x}$$

the  $x$ -axis, and

the line  $x = 5$

Each cross-section of the solid perpendicular to the  $x$ -axis is a square, with one side on the  $xy$ -plane. Which of the following expressions represents the volume of the solid?

a)  $\int_0^5 5x \, dx$

b)  $\int_0^5 5\sqrt{x} \, dx$

c)  $\int_0^5 25x \, dx$

d)  $\int_0^1 25x \, dx$

e)  $\int_0^1 5\sqrt{x} \, dx$

41) The rate at which a bacteria population grows is proportional to the number of bacteria present. Initially, there were 1000 bacteria present and the population doubled in 4 hours. Roughly how many hours does it take for the population to reach 10000?

a) 13.2

b) 16.4

c) 20.8

d) 8.8

e) 11.6

42) Given that  $F'(x) = f(x)$ , find

$$\int_0^6 x f(x^2) \, dx$$

a)  $6 F(36)$

b)  $\frac{F(36) - F(0)}{(2)}$

c)  $2 F(\sqrt{6}) - 2 F(0)$

d)  $\frac{36 F(36)}{(2)}$

e)  $2 F(36) - 2 F(0)$

43) The line normal to

$$5x^2 + 4y + y^2 = 3$$

at  $x = m$  is parallel to the  $y$ -axis. What is  $m$ ?

a) -2

b) 0

c) 5

d) -5

e) 2

44)  $f$  and  $g$  are two differentiable functions such that

$$\begin{aligned} f(1) &= g(1) = 4 \\ f'(1) &= g'(1) = 6 \end{aligned}$$

$$f'(4) = 4$$

$$g'(4) = 6$$

If  $h(x) = (f \circ g)(x)$ , then  $h'(1)$  is

a) 24

b) 6

c) 16

d) 36

e) 1

45) If  $\frac{dy}{dx} = ye^x$  and  $y(0) = 6$ , then  $y \ln(2) =$

a)  $6e^{-2}$

b)  $6e^2$

c)  $6e^3$

d)  $6e^{-1}$

e)  $6e$

1) Find

$$\lim_{h \rightarrow 0} \left( \frac{\sin(4x + 4h) - \sin(4x)}{h} \right)$$

a)  $-4 \sin(4x)$

b)  $0$

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\*d)  $4 \cos(4x)$

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Find the slope of the tangent line at  $x = 1$ .

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b)  $3e^3$

c)  $\frac{1}{3}e^3$

d)  $\frac{1}{3}(e^3 - 1)$

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3) Find

$$\lim_{x \rightarrow \infty} \left( \frac{3x - 1}{\sqrt{x^2 + 9}} \right)$$

\*a)  $3$

b)  $\frac{1}{3}$

c)  $1$

d)  $-\frac{1}{9}$

e) The limit does not exist.

4) The given function  $f$  has a removable discontinuity at  $x = -5$ . Find  $A$ .

$$f(x) = \begin{cases} 5x^2 + 8 & x < -5 \\ 8x & x = -5 \\ Ax + 8 & -5 < x \end{cases}$$

a)  $-4$

b)  $5$

c)  $-15$

\*d)  $-25$

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5) If  $f'(x) = -5(x-4)^2(x-8)$  which of the following is true about  $y = f(x)$ ?

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c)  $\frac{1}{21}e^{21}$

d)  $\frac{1}{3}(e^{21} - 1)$

e)  $\frac{1}{7}e^{21}$

8) Find  $f'(0)$ , given that

$$f(x) = 2^x \ln(5e^x)$$

a)  $\ln(5) + 1$

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9) Find  $f'(1)$ , given that

$$f(x) = \frac{x^2 + 7}{(8x)}$$

a)  $\frac{15}{64}$

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10) Find

$$\lim_{x \rightarrow 0} \left( \frac{\sin(8x) \cos(x) - \sin(x) \cos(8x)}{x^2} \right)$$

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d)  $5\sin(5x)$

e)  $-5\sin^{-1}(5x)$

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$$\frac{\partial}{\partial x} \left( \int_2^x \ln(4+t) dt \right)$$

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d)  $\frac{1}{4 + x}$

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16) Find the equation of the tangent line to the given curve at the point (0, 7).

$$y = 5x^2 + 10x + 7$$

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d)  $y = -5x + 7$

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a)  $-\frac{1}{4}$

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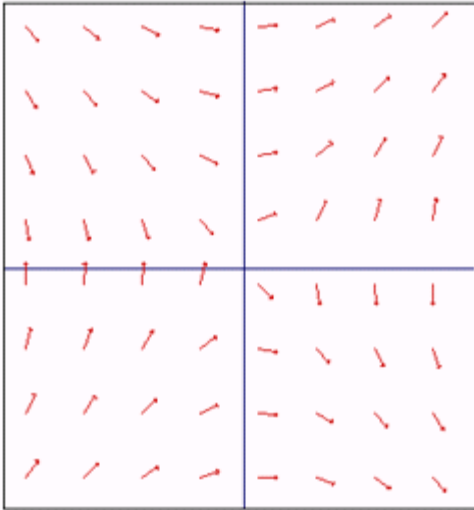
c)  $2m$

d)  $\frac{1}{2} m^2$

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19) Which of the following differential equations corresponds to the slope field shown in the figure below?





- a)  $\frac{dy}{dx} = -\frac{y}{x}$   
 b)  $\frac{dy}{dx} = \frac{1}{5}xy$   
 c)  $\frac{dy}{dx} = \frac{1}{10}xy$   
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$$f(x) = \frac{x}{\ln(7x)}$$

- a)  $\left(1, \frac{1}{7}e\right)$   
 b)  $\left(0, \frac{1}{7}\right)$   
 c)  $(1, 7)$   
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$$y = 2 \sin(x)$$

and the  $x$ -axis, for  $0 \leq x \leq \frac{1}{2} \pi$ , is rotated about the line  $y = -3$ . The volume of this solid can be represented

by:

a)  $2 \pi \int_0^{\frac{1}{2} \pi} (4 \sin(x)^2 + 3) dx$

\*b)  $\pi \int_0^{\frac{1}{2} \pi} ((2 \sin(x) + 3)^2 - 9) dx$

c)  $\pi \int_0^{\frac{1}{2} \pi} (4 \sin(x)^2 - 9) dx$

d)  $2 \pi \int_0^{\frac{1}{2} \pi} 4 \sin(3 + x)^2 dx$

e)  $2 \pi \int_0^{\frac{1}{2} \pi} (2 \sin(x) + 3)^2 dx$

24) The side of a cube is expanding at a constant rate of 5 inches per second. What is the rate of change of the volume, in  $in^3$  per second, when the total surface area of the cube is  $54 in^2$ ?

- a) 90
- b) 45
- \*c) 135
- d) 15
- e) 270

25) The solution to the differential equation

$$\frac{dy}{dx} = 4xy$$

with the initial condition  $y(0) = 6$  is

- a)  $6 \ln(2x^2)$
- b)  $e^{2x^2} + 5$
- c)  $\ln(2x^2 + 6)$

\*d)  $6 e^{2x^2}$

e)  $e^{2x^2} + 6$

26)  $\int \sec^2(6x) dx =$

a)  $\frac{1}{6} \tan^2(6x) + C$

b)  $-6 \tan(6x) + C$

c)  $6 \tan^2(6x) + C$

\*d)  $\frac{1}{6} \tan(6x) + C$

e)  $6 \tan(6x) + C$

27) The position of a particle moving along a horizontal line is given by

$$x(t) = 2(t-4)^3$$

What is the maximum speed of the particle for  $0 \leq t \leq 10$ ?

a) 384

b) 72

c) 96

d) 32

\*e) 216

28) Using the information below, find  $\frac{dz}{dt}$  when  $t = 0$ .

$$\begin{aligned} z &= \ln(y) \\ y &= 4x^2 + 4 \\ x &= 2t + 1 \end{aligned}$$

a)  $\frac{1}{4}$

b) 8

c) 16

d)  $\frac{1}{2}$

\*e) 2

29) If  $f$  is a differentiable function and  $f(0) = -3$  and  $f(5) = 6$ , then which of the following must be true?

- I. There exists a  $c$  in  $[0,5]$  where  $f(c) = 0$ .
- II. There exists a  $c$  in  $[0,5]$  where  $f'(c) = 0$ .
- III. There exists a  $c$  in  $[0,5]$  where  $f'(c) = 9/5$ .

- a) I, II and III
- b) II only
- c) II and III only
- \*d) I and III only
- e) I only

30) Which of the following function(s) is continuous and differentiable?

I.  $f(x) = \frac{8}{\sqrt{x}}$

II.  $g(x) = x|x|$

III.  $h(x) = \begin{cases} 6x + 1 & x \leq 0 \\ x^2 + 1 & 0 < x \end{cases}$

- a) I only
- b) II only
- c) III only
- \*d) I and II only
- e) I and III only

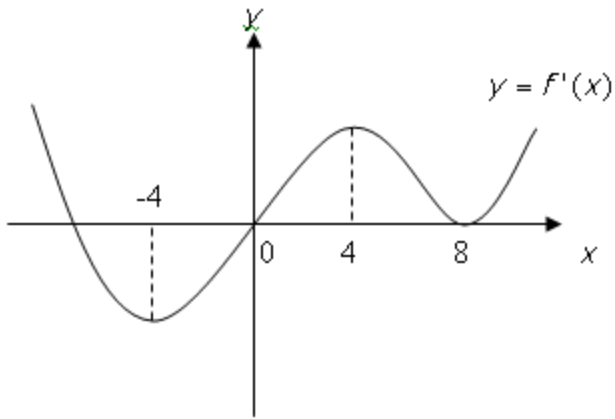
31) The area of the region in the first quadrant bounded by the graphs of  $y = 3\cos(x)$ ,  $y = 3\sin(x)$ , and the  $y$ -axis is

- \*a)  $3(\sqrt{2} - 1)$
- b)  $\frac{3}{2}\sqrt{2}$
- c) 6
- d)  $3\sqrt{2} + 1$
- e)  $3\sqrt{2}$

32) Air is pumped into a spherical balloon at a rate of  $9\text{cm}^3$  per second. At what rate is the radius of the sphere changing when its volume is  $36\pi\text{cm}^3$ ? 

- a)  $\frac{1}{8\pi}$  cm/sec
- b)  $\frac{3}{8\pi}$  cm/sec
- c)  $\frac{1}{\pi}$  cm/sec
- \*d)  $\frac{1}{4\pi}$  cm/sec
- e)  $\frac{3}{\pi}$  cm/sec

33) The graph of the derivative of  $f$  is shown below. Which of the following must be true?



- a)  $f$  has a local minimum at  $x = -4$ .
- b)  $f$  has a local maximum at  $x = 0$ .
- c)  $f$  is concave down on  $[0, 8]$ .
- \*d)  $f$  has a point of inflection at  $x = 8$ .
- e)  $f$  is increasing on  $[-4, 4]$ .

34) A particle is moving along the  $x$ -axis and its position at time  $t \geq 0$  is given by

$$S(t) = (t-3)^2 (t-6)$$

Which of the following is (are) true?

- I. The particle changes direction at  $x = 3$  and  $x = 6$ .
  - II. The particle is slowing down on  $[0, 3]$ .
  - III. The particle is speeding up on  $[3, 6]$ .
- a) II and III only
  - b) I only
  - \*c) II only
  - d) I and III only
  - e) I, II and III

35) The region enclosed by the graphs of

$$y = 5e^x$$

and the line

$$y = 5$$

for  $0 \leq x \leq 1$ , is revolved about the  $y$ -axis. Which of the following integrals gives the volume generated?

- a)  $\pi \int_0^1 (5e^x - 5)^2 dx$
- \*b)  $\pi \int_5^{5e} \left( 1 - \left( \ln\left(\frac{1}{5}y\right) \right)^2 \right) dy$
- c)  $\pi \int_5^{5e} \left( 5 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$
- d)  $\pi \int_0^5 \left( 1 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$
- e)  $\pi \int_5^{5e} \left( 1 - \ln\left(\frac{1}{5}y\right) \right)^2 dy$

36) If

$$4x^2 + xy - \cos(y) = 10$$

then  $\frac{dy}{dx}$  is

- a)  $-\frac{8x}{x + \sin(y)}$
- b)  $\frac{y - 8x}{x - \sin(y)}$
- \*c)  $-\frac{(y + 8x)}{x + \sin(y)}$
- d)  $\frac{y + x}{x - \sin(y)}$
- e)  $-\frac{(x + \sin(y))}{y + 8x}$

37) The sum of two positive integers  $x$  and  $y$  is 60. Find the value of  $x$  that minimizes

$$P = x^3 - 60xy$$

- a)  $x = 30$
- \*b)  $x = 20$
- c)  $x = 10$
- d)  $x = 50$
- e)  $x = 40$

38) A particle moves along a straight line, and its velocity at time  $t$  is given by

$$v(t) = 4 - \ln(t)$$

What is the total distance the particle travels from  $t = 1$  to  $t = e$ ?

- a)  $4e + 4$
- b)  $4e - 1$
- c)  $4e + 1$
- d)  $e - 5$
- \*e)  $4e - 5$

39) The function  $f$  is defined as

$$f(x) = \frac{(x-5)^2}{x-6}$$

$$x \neq 6$$

Which of the following is **false**?

- a)  $f$  is decreasing on  $[5, 6]$ .
- b)  $f$  has a vertical asymptote at  $x = 6$ .
- \*c)  $f$  has a horizontal asymptote at  $y = 1$ .
- d)  $f$  has a local maximum at  $x = 5$ .
- e)  $f$  is concave up for  $x > 6$ .

40) The base of a solid is the region bounded by

$$y = 5\sqrt{x}$$

the  $x$ -axis, and

the line  $x = 5$

Each cross-section of the solid perpendicular to the  $x$ -axis is a square, with one side on the  $xy$ -plane. Which of the following expressions represents the volume of the solid?

a)  $\int_0^5 5x \, dx$

b)  $\int_0^5 5\sqrt{x} \, dx$

\*c)  $\int_0^5 25x \, dx$

d)  $\int_0^1 25x \, dx$

e)  $\int_0^1 5\sqrt{x} \, dx$

41) The rate at which a bacteria population grows is proportional to the number of bacteria present. Initially, there were 1000 bacteria present and the population doubled in 4 hours. Roughly how many hours does it take for the population to reach 10000?

\*a) 13.2

b) 16.4

c) 20.8

d) 8.8

e) 11.6

42) Given that  $F'(x) = f(x)$ , find

$$\int_0^6 x f(x^2) \, dx$$

a)  $6F(36)$

\*b)  $\frac{F(36) - F(0)}{(2)}$

c)  $2F(\sqrt{6}) - 2F(0)$

d)  $\frac{36F(36)}{(2)}$

e)  $2F(36) - 2F(0)$

43) The line normal to

$$5x^2 + 4y + y^2 = 3$$

at  $x = m$  is parallel to the  $y$ -axis. What is  $m$ ?

a)  $-2$

\*b)  $0$

c)  $5$

d)  $-5$

e)  $2$

44)  $f$  and  $g$  are two differentiable functions such that

$$\begin{aligned} f(1) &= g(1) = 4 \\ f'(1) &= g'(1) = 6 \end{aligned}$$

$$f'(4) = 4$$

$$g'(4) = 6$$

If  $h(x) = (f \circ g)(x)$ , then  $h'(1)$  is

\*a) 24

b) 6

c) 16

d) 36

e) 1

45) If  $\frac{dy}{dx} = ye^x$  and  $y(0) = 6$ , then  $y \ln(2) =$

a)  $6e^{-2}$

b)  $6e^2$

c)  $6e^3$

d)  $6e^{-1}$

\*e)  $6e$