AP Calculus AB/BC |

SCORE SHEET

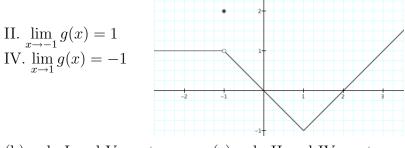
Part I			<u>Part II</u>				
1:		9:		1:		9:	
2:		10:		2:		10:	
3:		11:		3:		11:	
4:		12:		4:		12:	
5:		13:		5:		13:	
6:		14:		6:		14:	
7:		15:		7:		15:	
8:		16:		8:		16:	

PART I - 16 problems

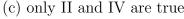
1. Find
$$\lim_{x \to 2} \frac{x-2}{x^2-x-2}$$
.
(a) 0
(b) 3
(c) $\frac{1}{2}$
2. Find $\lim_{x \to 2} \frac{x^3-5}{4x^3+x+1}$.

$$x \to +\infty \ 4x^{3} + x + 1$$
(a) $\frac{3}{4}$
(b) $\frac{1}{4}$
(c) 1
(d) 0
(e) $+\infty$

- AP Calculus AB/BC |
- 3. Find $\lim_{x \to -\infty} e^x$.
 - (a) 0 (b) *e* (c) 1 (e) $-\infty$ (d) $+\infty$
- 4. The graph of a function g(x) is shown below. Which of the following statements are true of g(x)?
 - I. $\lim_{x \to -1} g(x) = 2$ III. $\lim_{x \to -1} g(x)$ does not exist V. $\lim_{x \to 1} g(x)$ does not exist



(b) only I and V are true (e) only III and V are true



5. f'(x) can be defined as:

(a) only I and IV are true

(d) only II and V are true

(a)
$$\lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{x}$$
 (b)
$$\lim_{x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$
 (c)
$$\lim_{x \to \Delta x} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

(d)
$$\lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$
 (e) none of the above

6. Consider again the function q(x) whose graph is shown in problem 4. Which of the following statements are true of q(x)?

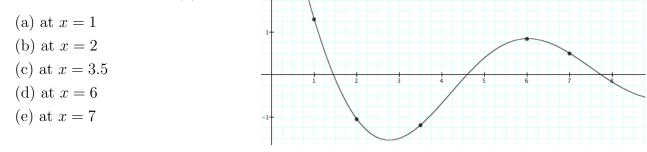
I. q is continuous at x = -1III. g is differentiable at x = -1V. q is differentiable at x = 1

II. q is continuous at x = 1IV. q is differentiable at x = 0

(a) only I and IV are true (d) only II and V are true (b) only II and IV are true (e) only III and V are true

(c) only I and V are true

7. The graph of a function f(x) is shown below. At which of the following points is the value of the derivative f'(x) biggest?



8. Consider again the function f(x) whose graph is shown in problem 7. At which points is the second derivative f''(x) negative?

(a) at x = 2 and x = 3.5(b) at x = 1, x = 2 and x = 3.5(c) at x = 6 only (e) at x = 6 and x = 7(d) at x = 7 only

9. Let
$$f(x) = \ln x \cdot \cos x$$
. Find $f'(x)$.

(a)
$$\frac{1}{\cos x} \cdot (-\sin x)$$
 (b) $\frac{1}{x} \cdot (-\sin x)$ (c) $\frac{1}{x} \cos x - \ln x \sin x$
(d) $\frac{1}{x \cos x} (\cos x - x \sin x)$ (e) none of the above
10. Let $u = 4e^{\tan x}$ Find $\frac{dy}{dx}$

(a)
$$4e^{\tan x} \cdot \sec^2 x$$

(b) $4e^{\tan x} \cdot \frac{1}{1+x^2}$
(c) $4e^{\tan x}$
(c) $4e^{\tan x}$

11. Let $f(x) = \sin^{-1} x$. Find f'(0).

(a)
$$\pi$$
 (b) 1 (c) $\frac{1}{2}$
(d) 0 (e) none of the above

12. The equation of the line tangent to the graph of $f(x) = x^2 + 5x$ at the point with x-coordinate x = 2 is:

(a)
$$y = 9x - 14$$
 (b) $y = 9x$ (c) $y = 9x - 4$
(d) $y = -\frac{1}{9}x - \frac{2}{9}$ (e) none of the above

13. Let $f(x) = x^3 - 3x$. Which of the following statements are true?

I. f(x) has local maxima at both x = -1 and x = 1. II. f(x) has a local minimum at x = 1 and an inflection point at x = 0. III. f(x) has both a local minimum and an inflection point at x = 0.

- (a) only I is true(b) only II is true(c) only III is true(d) only I and III are true(e) none of the statements is true
- 14. A commercial nursery has 1000 yards of fencing which the owners plan to use to enclose as large a rectangular garden as possible. The garden will be bounded on one side by a barn, so no fencing is needed on that side. How large will the garden be (in square yards)?

15. The width of a rectangle is increasing at a rate of 2 cm/sec, and its length is increasing at a rate of 3 cm/sec. At what rate is the area of the rectangle increasing when its width is 4 cm and its length is 5 cm?

(a) $31 \text{ cm}^2/\text{sec}$	(b) $23 \text{ cm}^2/\text{sec}$	(c) $5 \text{ cm}^2/\text{sec}$
(d) $22 \text{ cm}^2/\text{sec}$	(e) none of the above	

AP Calculus AB/BC

- 16. A rock is dropped from a height of 400 feet and falls toward the earth in a straight line; t seconds after it is dropped, it has fallen a distance of $s(t) = 16t^2$ feet. At what speed is the rock traveling when it hits the ground?
 - (a) 20 ft/sec (b) 32 ft/sec (c) 640 ft/sec (c) 640 ft/sec

PART II - 16 problems

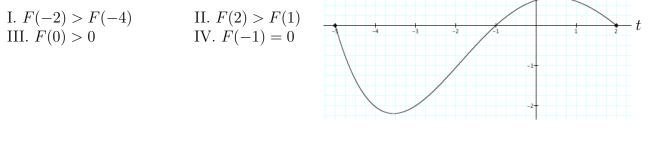
- 1. Which of the following gives the area between the curves $y = x^2$ and y = 2x over the interval [-2, 2]?
 - (a) $\int_{-2}^{2} (x^2 2x) dx$ (b) $\int_{-2}^{2} (2x x^2) dx$ (c) $\int_{-2}^{0} (x^2 2x) dx + \int_{0}^{2} (2x x^2) dx$ (d) $\left| \int_{-2}^{2} (x^2 - 2x) dx \right|$ (e) none of the above
- 2. Suppose that f(x) is a continuous function with the following properties: $f''(x) = \cos x$, $f'(\pi) = 2$ and f(0) = 4. What is $f(\pi)$?
 - (a) 2 (b) 2π (c) $\pi + 2$ (d) $6 + 2\pi$ (e) 0

3. Suppose that the function f(x) is defined by $f(x) = \int_1^x \frac{e^t}{t} dt$. Find f'(x).

(a) $e^x \ln x$ (b) $e^x \ln x - \frac{e^x}{x}$ (c) $\frac{e^x}{x}$

(d) $\frac{e^x}{x} - e$ (e) the integral can't be computed, so it's impossible to give the answer

4. Let $F(x) = \int_0^x f(t) dt$, where f(t) is the function shown below. Which of the following statements are true?



(a) only I is true(b) only II is true(c) only III is true(d) only I and II are true(e) only II and IV are true

AP Calculus AB/BC |
5. Suppose that
$$f(x) = \frac{x}{x^2 + 1}$$
. Find $\int_0^2 f'(x) dx$.
(a) $\frac{2}{5}$ (b) $-\frac{28}{25}$ (c) $\frac{28}{25}$
(d) 0 (e) none of the above

6. Which of the following statements about indefinite integrals are true?

I.
$$\int f(x) + g(x) \, dx = \int f(x) \, dx + \int g(x) \, dx$$
 II. $\int f(x)g(x) \, dx = \int f(x) \, dx \cdot \int g(x) \, dx$
III. $\int f'(g(x))g'(x) \, dx = f(g(x)) + C$ IV. $\int [f(x)]^n \, dx = \frac{[f(x)]^{n+1}}{n+1} + C$

- (a) only I and II are true
- (d) only I, II and IV are true

(b) only I and III are true(c) only I and IV are true(e) only I, III and IV are true

7. Find the volume of the solid obtained by rotating the region bounded by $y = x^2$ and y = x over the interval [0, 1] around the x-axis.

(a)
$$\int_0^1 \pi (x^2 - x^4) dx$$
 (b) $\int_0^1 \pi (x - x^2)^2 dx$ (c) $\int_0^1 \pi (x^2 - x^4)^2 dx$
(d) $\int_0^1 \pi (\sqrt{y} - y) dy$ (e) $\int_0^1 \pi (y - y^2) dy$

8. The integral $\int \frac{1}{x \ln x} dx$ can be found by

- (a) making the substitution $u = \ln x$
- (b) making the substitution $u = \frac{1}{x}$
- (c) using integration by parts, with $u = \ln x$ and dv = x
- (d) taking the reciprocal of $\int x \ln x \, dx$
- (e) none of the above
- 9. The integral $\int x \sin x \, dx$ can be found by
 - (a) making the substitution u = x
 - (b) making the substitution $u = \sin x$
 - (c) using integration by parts, with $u = \sin x$ and dv = x dx
 - (d) using integration by parts, with u = x and $dv = \sin x \, dx$
 - (e) none of the above

10. Find
$$\int_{0}^{\ln\sqrt{3}} \frac{e^{x}}{1+e^{2x}} dx$$

(a) $\ln 2$ (b) 1 (c) $\frac{\pi}{12}$
(d) $\frac{\pi}{4}$ (e) 0

11. Find
$$\lim_{x \to 0} \frac{\operatorname{APCalculus} \operatorname{AB/BC}}{x^3}$$
.
(a) 0 (b) 1 (c) $\frac{1}{6}$ (c) $\frac{1}{6}$

12. Find
$$\int_{1}^{\infty} \frac{1}{x^2} dx$$
.
(a) 1 (b) 2 (c) 10
(d) 20 (e) the integral diverges

13. Which of the following improper integrals converge to a finite value?

(I)
$$\int_{1}^{\infty} e^{-x} dx$$
 (II) $\int_{-\infty}^{\infty} x^{3} dx$ (III) $\int_{-\infty}^{\infty} \frac{1}{1+x^{2}} dx$
(a) I only (b) III only (c) I and II only (d) I and III only (e) all of them

14. The second order Taylor polynomial at x = 0 for $f(x) = e^{-x}$ is

(a)
$$1 - \frac{x^2}{2}$$
 (b) $1 + \frac{x^2}{2}$ (c) $1 + x + \frac{x^2}{2}$
(d) $1 - x + x^2$ (e) $1 - x + \frac{x^2}{2}$

15. Which of the following series converge?

(I)
$$\sum_{n=1}^{\infty} \frac{1}{n^2}$$
 (II) $\sum_{n=1}^{\infty} \frac{1}{n}$ (III) $\sum_{n=1}^{\infty} \frac{n}{2^n}$

(a) (I) only(b) (III) only(c) (I) and (II) only(d) (I) and (III) only(e) all of them

16. The radius of convergence of the power series $\sum_{n=0}^{\infty} x^n$ is

- (a) 0 (b) 1 (c) 2
- (d) 3 (e) ∞